Experimental and Theoretical Investigation of the UV Spectrum and Kinetics of the Aminomethyl Radical, \( \cdot \text{CH}_2\text{NH}_2 \)

Thomas la Cour Jansen,\(^a,\)* Ib Trabjerg,\(^a\) Sten Retrup,\(^a\) Palle Pagsberg\(^b\) and Alfred Sillesen\(^b\)

\(^a\)Department of Chemistry, University of Copenhagen, Universitetsparken 5, DK-2100 Copenhagen Ø, Denmark and \(^b\)Chemical Reactivity Section, Plant Biology and Biogeochemistry Department, Risø National Laboratory, DK 4000 Roskilde, Denmark


The aminomethyl radical was produced by the reaction \( \cdot \text{CH}_2\text{NH}_2 \rightarrow \cdot \text{H} + \text{CH}_3\text{NH} \), which was initiated by pulse radiolysis of \( \text{CH}_3\text{NH}_2 \cdot \text{SF}_6 \) mixtures. The ultraviolet absorption spectrum of \( \text{CH}_3\text{NH}_2 \) was recorded on a timescale of 2 ps using a gated optical multichannel analyzer. The vibronic structure observed in the range 270–380 nm was analyzed by comparison with the results of \textit{ab initio} calculations. Kinetics of the self-reaction \( 2 \cdot \text{CH}_2\text{NH}_2 \rightarrow \text{products} \) was studied by monitoring the transient absorption of \( \cdot \text{CH}_2\text{NH}_2 \) at 319.5 nm. A value of \( k = 8.1 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \) was derived from the observed second-order kinetics combined with an estimated yield of the radical. In the presence of oxygen the decay rate was found to increase in accordance with the reaction \( \cdot \text{CH}_2\text{NH}_2 + \text{O}_2 \rightarrow \text{products} \) proceeding with a rate constant of \( 7.8(8) \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \).

Oxidation of methyamine in the atmosphere is initiated by reaction with hydroxyl radicals, and has been studied previously by monitoring the decay rate of \( \cdot \text{OH} \).

\[
\begin{align*}
\cdot \text{OH} + \text{CH}_3\text{NH}_2 & \rightarrow \cdot \text{H}_2\text{O} + \cdot \text{CH}_2\text{NH}_2 \\
\cdot \text{OH} + \text{CH}_3\text{NH}_2 & \rightarrow \cdot \text{H}_2\text{O} + \text{CH}_3\text{NH}
\end{align*}
\]

(1a) \hspace{5cm} (1b)

Because of the difference in bond energies,

\[
D(\text{H–CH}_2\text{NH}_2) = 94.6(2.0) \text{ kcal mol}^{-1}
\]

and

\[
D(\text{CH}_3\text{NH–H}) = 103(2) \text{ kcal mol}^{-1}
\]

it is proposed that reaction (1a) predominates. Based on an overall rate constant of \( k_1 = 2.2 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \) at 299 K the tropospheric lifetime of \( \text{CH}_3\text{NH}_2 \) was estimated to be about 3 h. The following reactions of \( \text{CH}_3\text{NH}_2 \) with \( \text{O}_2 \) and \( \text{NO} \) have been proposed.

\[
\begin{align*}
\text{CH}_3\text{NH}_2 + \text{O}_2 & \rightarrow \cdot \text{OOCCH}_2\text{NH}_2 \\
\cdot \text{OOCCH}_2\text{NH}_2 + \text{NO} & \rightarrow \cdot \text{OCH}_2\text{NH}_2 + \text{NO}_2 \\
\cdot \text{OCH}_2\text{NH}_2 & \rightarrow \text{HCHO} + \cdot \text{NH}_2 \\
\cdot \text{OCH}_2\text{NH}_2 + \text{O}_2 & \rightarrow \cdot \text{OCHNH}_2 + \text{HO}_2
\end{align*}
\]

(2) \hspace{5cm} (3) \hspace{5cm} (4) \hspace{5cm} (5)

*To whom correspondence should be addressed.

The radical \( \cdot \text{CH}_2\text{NH}_2 \) produced by pulsed laser photolysis of ethylenediamine has been observed by photoionization mass spectrometry and a value of \( k_2 = 3.5 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \) has been reported. In the present investigation we have recorded the ultraviolet spectrum of \( \cdot \text{CH}_2\text{NH}_2 \) produced in the reaction of \( \text{F} \)-atoms with methyamine. The spectral features have been analyzed by \textit{ab initio} calculations.

**Experimental**

The experimental set-up for pulse radiolysis combined with time-resolved ultraviolet spectroscopy has previously been described in detail.\(^5\) High yields of \( \text{F} \)-atoms were obtained by radiolysis of \( \text{SF}_6 \), which was used as bath gas with a total pressure of 1 atm. In the presence of a small mole fraction of methyamine all \( \text{F} \)-atoms reacted by abstraction of H-atoms producing radicals of which only \( \cdot \text{CH}_2\text{NH}_2 \) was identified. The ultraviolet spectrum of \( \text{CH}_2\text{NH}_2 \) was recorded with an optical multichannel analyzer on a timescale of a few microseconds. Kinetic studies were carried out by monitoring the transient absorption of \( \cdot \text{CH}_2\text{NH}_2 \) at 319.5 nm.
UV spectrum of \(\text{CH}_2\text{NH}_3\). Reactions (6a) and (6b) were initiated by pulse radiolysis of SF\(_6\) containing a small mole fraction of methylamine.

\[
\begin{align*}
F^- + \text{CH}_2\text{NH}_3 &\rightarrow \text{HF} + \text{CH}_2\text{NH}_2 \quad (6a) \\
F^- + \text{CH}_2\text{NH}_3 &\rightarrow \text{HF} + \cdot\text{CH}_2\text{NH} \quad (6b)
\end{align*}
\]

Figure 1 shows the ultraviolet spectrum of a short-lived radical which has been assigned the structure \(\text{CH}_2\text{NH}_2\). The spectrum was recorded with an optical multichannel analyzer on a timescale of 2 \(\mu\)s. The electronic transitions of \(\text{CH}_2\text{NH}_2\) appear to be similar to the Rydberg transitions of the isoelectronic radical \(\text{CH}_2\text{OH}\).\(^5\)\(^6\) Based on the relative intensities and the bandshapes of the vibronic progression it seems obvious that at least two different electronic transitions are involved. The low energy transition \(\text{a}^{'}\) with the 0–0 band situated at 368.6 nm is composed of a fairly strong vibronic progression with an average spacing of \(\Delta \nu = 830 \text{ cm}^{-1}\). The strong 0–0 band \(\text{b}^{'}\) at 319.5 nm was identified as the origin of a stronger electronic transition involving a complex mixture of vibronic progressions coupled with sharp antiresonances. A detailed analysis of the spectral features is presented in the theoretical section.

Kinetics of \(\text{CH}_2\text{NH}_2\). The kinetics of \(\text{CH}_2\text{NH}_2\) were studied by monitoring the transient absorption at 319.52 nm. Figure 2 shows the kinetics of the self-reaction of \(\text{CH}_2\text{NH}_2\), which is most likely a combination reaction (7a) although the disproportionation reaction (7b) cannot be ruled out.

\[
\begin{align*}
\text{CH}_2\text{NH}_2 + \text{CH}_2\text{NH}_2 &\rightarrow \text{H}_2\text{N}^+ - \text{CH}_2\text{CH}_2\text{NH}_2 \quad (7a) \\
\text{CH}_2\text{NH}_2 + \text{CH}_2\text{NH}_1 &\rightarrow \text{CH}_3\text{NH}_2 + \text{CH}_2\text{NH} \quad (7b)
\end{align*}
\]

Based on reported values of \(\Delta H_{298}/\text{kcal mol}^{-1}\) for \(\text{CH}_2\text{NH}_2\) \((33.5)\)\(^5\)\(^6\), \(\text{CH}_2\text{NH}_2\) \((-5.5)\)\(^8\) and \(\text{CH}_2\text{NH}\) (22)\(^10\) reaction (7b) should be exothermic by about 50 kcal mol\(^{-1}\). The kinetic features were analyzed by computer modeling using the CHEMSIMUL program.\(^1\)\(^1\) By use of a simple model including only the reaction (6a) and (7a) the experimental curve shown in Fig. 2 could be fitted within the signal-to-noise ratio after adjustment of the rate constants, \(k_{\text{a}} = 1.3 \times 10^{-10} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}\) and \(k_{\text{g}} = 8.1 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}\). The value of \(k_{\text{a}}\) may be taken with confidence while the value of \(k_{\text{g}}\) represents a lower limit based on the assumption that all F-atoms are consumed in reaction (6a).

In the presence of oxygen the decay rate of \(\text{CH}_2\text{NH}_2\) was found to increase with increasing oxygen concentrations, as shown in Fig. 2b. The addition reaction (8a) was proposed by Atkinson\(^2\) while the formation of methyleneimine via (8b) has been discussed by Schade and Crutzen.\(^3\)

\[
\begin{align*}
\text{CH}_2\text{NH}_2 + \text{O}_2 &\rightarrow \cdot\text{OOCH}_2\text{NH}_2 + \text{M} \quad (8a) \\
\text{CH}_2\text{NH}_2 + \text{O}_2 &\rightarrow \text{CH}_3\text{NH} + \text{HO}_2 \quad (8b)
\end{align*}
\]

The decay rate of the radical was studied as a function of oxygen concentration in the range \(p(\text{O}_2)\) = 0.5–1.5 mbar, and, based on computer simulations of the experimental curves, we have determined a value of \(k_8 = k_{8a} + k_{8b} = 7.8 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}\) at a total pressure of 1 atm. This value may be compared with the value of \(k_8 = 3.5 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1}\) determined by Washida et al. at total pressures in the range 0.6–6 Torr,\(^12\) where the overall rate constant was found to remain constant. However, the difference between the rate constants obtained at different pressures may be taken as evidence for the occurrence of the pressure-dependent reaction (8a). Schade and Crutzen\(^13\) have proposed that reaction (8b) may be a major channel in the atmospheric oxidation mechanism of methylamine. In the case of methanol we observed the analogous reaction \(\text{CH}_3\text{OH} + \text{O}_2 \rightarrow \text{CH}_2\text{O} + \text{HO}_2\).\(^14\) Thus, it appears that both reactions (8a) and (8b) contribute to the atmospheric oxidation of methylamine. Oxidation of
the intermediate product methyleneimine may give rise to the formation of HCN and N₂O, which we intend to study by another experimental technique based on pulse radiolysis combined with infrared diode laser spectroscopy. Formation and decay of the intermediate CH₂NH may be studied by scanning characteristic regions of the IR spectrum.

Theoretical

Properties of CH₂NH₂ in the ground state. Ab initio calculations were carried out using a basis set consisting of primitive Gaussian functions (C,N/13,8,3) and (H/4) contracted as \langle C,N/7,6,3 \rangle and \langle H/2 \rangle with spherical components of the d functions included in the calculation. These functions are the s, p and d functions from the VTZ basis set from the MOLPRO basis set library for C and N and the s functions from the DZ basis set by Dunning for H. The basis set was augmented with 3 primitive s, 3 primitive p and 1 primitive d functions on the heavy atoms; these are sufficient to ensure a good description of the Rydberg states (Table 1). In total the basis set consisted of 88 contracted functions. The geometry of CH₂NH₂ has been calculated with the Restricted Open-shell Hartree-Fock (ROHF) method.

The ground state geometry, with C₄ symmetry presented in Cartesian coordinates in Table 2, is similar to the geometry found previously by Dyke et al. The vertical ionization potential was estimated to be 6.6 eV based on the SCF method. The excitation energies were calculated with the same basis set and the geometry derived by the ROHF method using Multi Reference Configuration Interaction (MRCI) with reference functions from an intermediate Complete Active Space Self Consistent Field (CASSCF) calculation with the six states of lowest energy as reference states: four with \( A' \) symmetry and two with \( A'' \) symmetry. The complete active space had three electrons in six active orbitals resulting in 55 determinants of \( A' \) symmetry and 35 of \( A'' \) symmetry. The six states were optimized with equal weight and identified using symmetry and energy considerations. The MRCl calculation optimized the same six states with equal weight using single and double excitation in the entire space resulting in 417 206 configurations for calculations on \( A' \) symmetry states and 412 454 for \( A'' \) symmetry states. The calculations were done using the program package MOLPRO. The vibrational frequencies for the ground state have been calculated using the TVZP basis set used by Dyke et al. This calculation was performed with CADPAC and the values here calculated at the SCF level are shown in Table 3. The vibrational frequencies calculated in this way are usually expected to be approximately 10% too high.

Excitation energies and oscillator strengths for various Rydberg transitions. Figure 3 shows the UV spectrum of CH₂NH₂ on a wavenumber scale. The low energy part of the spectrum in the range of 27 127–31 000 cm⁻¹ is

Table 1. Exponents for diffuse functions in the basis set.

<table>
<thead>
<tr>
<th>Carbon</th>
<th>Nitrogen</th>
</tr>
</thead>
<tbody>
<tr>
<td>Function</td>
<td>Exponent</td>
</tr>
<tr>
<td>s</td>
<td>0.044020</td>
</tr>
<tr>
<td>s</td>
<td>0.015000</td>
</tr>
<tr>
<td>s</td>
<td>0.005166</td>
</tr>
<tr>
<td>p</td>
<td>0.035680</td>
</tr>
<tr>
<td>p</td>
<td>0.010536</td>
</tr>
<tr>
<td>p</td>
<td>0.003110</td>
</tr>
<tr>
<td>d</td>
<td>0.100000</td>
</tr>
</tbody>
</table>

Table 2. The geometry of CH₂NH₂ in Cartesian coordinates (atomic units).

<table>
<thead>
<tr>
<th>Atom</th>
<th>x</th>
<th>y</th>
<th>z</th>
</tr>
</thead>
<tbody>
<tr>
<td>C</td>
<td>0.000000000</td>
<td>0.000000000</td>
<td>0.000000000</td>
</tr>
<tr>
<td>N</td>
<td>2.583093906</td>
<td>0.000000000</td>
<td>0.000000000</td>
</tr>
<tr>
<td>H1</td>
<td>-0.927206002</td>
<td>0.502291695</td>
<td>-1.753583606</td>
</tr>
<tr>
<td>H2</td>
<td>-0.927206002</td>
<td>0.502291695</td>
<td>1.753583606</td>
</tr>
<tr>
<td>H3</td>
<td>3.428970380</td>
<td>-0.639031080</td>
<td>1.568880032</td>
</tr>
<tr>
<td>H4</td>
<td>3.428970380</td>
<td>-0.639031080</td>
<td>-1.568880032</td>
</tr>
</tbody>
</table>

Fig. 3. UV spectrum of CH₂NH₂. Band heads of the Rydberg transitions are located at 27.127 cm⁻¹ (π* → 3pₓ) and 31.300 cm⁻¹ (π* → 3pᵧ). The complex vibrational structure of the π* → 3pᵧ Rydberg transition is presented in Table 5.
Table 4. Electronic transitions from the ground state of \( \text{CH}_2\text{NH}_2 \).

<table>
<thead>
<tr>
<th>Type of transition</th>
<th>Excitation energy/cm(^{-1})</th>
<th>Oscillator strength</th>
<th>Wavelength/nm</th>
</tr>
</thead>
<tbody>
<tr>
<td>( \pi^* \rightarrow 3s )</td>
<td>20 240</td>
<td>( 38 \times 10^{-5} )</td>
<td>494</td>
</tr>
<tr>
<td>( \pi^* \rightarrow 3p_x )</td>
<td>27 580</td>
<td>( 78 \times 10^{-5} )</td>
<td>363</td>
</tr>
<tr>
<td>( \pi^* \rightarrow 3p_y )</td>
<td>28 160</td>
<td>( 5 \times 10^{-5} )</td>
<td>355</td>
</tr>
<tr>
<td>( \pi^* \rightarrow 3p_z )</td>
<td>30 710</td>
<td>( 1430 \times 10^{-5} )</td>
<td>326</td>
</tr>
</tbody>
</table>

composed of a vibronic progression with band shapes that are clearly different from sharp bands occurring at 31.296 cm\(^{-1}\) and above. Thus, it appears that at least two different Rydberg transitions are involved, as in the case of the isoelectronic radical \( \text{CH}_2\text{OH} \).\(^{5,6}\) A simple analysis based on the Rydberg equation, \( E/\text{eV} = IP - 13.6/(n-\delta)^2 \) may be used to identify the electronic transition.

With \( \pi^* = 3 \) and \( \delta = 1 \) for a 3 Rydberg state combined with experimental values of the ionization potentials of 6.10 eV\(^{7}\) and 7.56 eV\(^{8}\) for \( \text{CH}_2\text{NH}_2 \) and \( \text{CH}_2\text{OH} \), we have calculated values of 2.70 eV and 4.16 eV, which may be compared with experimental values of 3.36 eV and 4.34 eV, respectively. Thus, in the case of \( \text{CH}_2\text{OH} \) the observed band head at 4.34 eV has been assigned to a \( \pi^* \rightarrow 3s \) Rydberg transition.\(^6\) However, in the case of \( \text{CH}_2\text{NH}_2 \) the observed transition at 3.36 eV does not coincide with the expected Rydberg transition at 2.70 eV. The excitation energies and oscillator strengths obtained by \( ab \text{ initio} \) calculations are presented in Table 4. The weak \( \pi^* \rightarrow 3s \) transition at 494 nm was not observed in the present investigation, but the wavelength is in agreement with the transition calculated using the Rydberg formula. However, the predicted stronger transitions \( \pi^* \rightarrow 3p_x \) and \( \pi^* \rightarrow 3p_y \) appear to be in good agreement with the experimental spectrum. The vibronic structure of the \( \pi^* \rightarrow 3p_z \) band may be expressed in terms of a main progression, \( \nu = 27 127 + \nu_1 \times 830 \text{ cm}^{-1} \) (\( \nu_1 = 0 - 4 \)). By comparison with the calculated frequencies in the ground state as shown in Table 3 it appears that a progression with \( \Delta \nu = 830 \text{ cm}^{-1} \) may be assigned to an out-of-plane bending mode.

The strong \( \pi^* \rightarrow 3p_z \) band starting at 31 300 cm\(^{-1}\) shows a complex vibronic structure containing sharp antiresonances.\(^{27}\) A number of vibronic transitions occur with an average spacing of 850 cm\(^{-1}\). However, the intensity distribution in the range of 31 300–33 000 cm\(^{-1}\) indicates that a progression with \( \Delta \nu = 1700 \text{ cm}^{-1} \) is more realistic.

As shown in Table 5 the strongest vibronic progression may be expressed by the simple linear equation, \( \nu = 31 300 + \nu_2 \times 1700 \text{ cm}^{-1} \), beginning at the band head as shown in Fig. 3. A similar progression, \( \nu = 32 150 + \nu_2 \times 1700 \text{ cm}^{-1} \) is displayed by \( \nu_2 = 850 \text{ cm}^{-1} \). The third progression, \( \nu = 31 900 + \nu_2 \times 850 \text{ cm}^{-1} \) with \( \nu_2 = 0 - 6 \), is displaced by \( \nu_4 = 600 \text{ cm}^{-1} \). The two progressions with \( \Delta \nu = 1700 \text{ cm}^{-1} \) may be assigned to either \( \text{NH}_2 \)-scissors or \( \text{CH}_2 \)-scissors by comparison with the calculated ground state frequencies listed in Table 3. Likewise the progression with \( \Delta \nu = 850 \text{ cm}^{-1} \) may be assigned to an \( \text{H}_2\text{C} = \text{NH}_2 \) trans-bend vibration. A number of weaker lines in the spectrum have not yet been assigned.

**Conclusions.** The UV spectrum of the aminomethyl radical, \( \text{CH}_2\text{NH}_2 \), has been recorded in the range 270–380 nm. Based on the results of \( ab \text{ initio} \) calculations we conclude that the spectrum is composed of two Rydberg transitions of which the low energy transition, \( \pi^* \rightarrow 3p_x \), starting at 368.6 nm is composed of a fairly strong vibronic progression with an average spacing of \( \Delta \nu = 830 \text{ cm}^{-1} \). The second Rydberg transition, \( \pi^* \rightarrow 3p_y \), starting at 319.5 nm shows a complex vibronic structure, which has tentatively been assigned to two displaced progressions with \( \Delta \nu = 1700 \text{ cm}^{-1} \) and one with \( \Delta \nu = 850 \text{ cm}^{-1} \). Kinetic studies of the formation and decay of \( \text{CH}_2\text{NH}_2 \) were carried out by monitoring the transient absorption at 319.52 nm. The formation reaction \( F^- + \text{CH}_2\text{NH}_2 \rightarrow \text{HF} + \text{CH}_2\text{NH}_2 \) was found to proceed with a rate constant of \( 1.3 \times 10^{-10} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \). A lower limit of \( 8.1 \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \) for the reaction \( 2 \text{CH}_2\text{NH}_2 \rightarrow \) products was derived from the observed second order kinetics based on the assumption that all F-atoms were consumed in the reaction \( F^- + \text{CH}_2\text{NH}_2 \rightarrow \text{HF} + \text{CH}_2\text{NH}_2 \). In the presence of oxygen the decay rate was found to increase in accordance with the reaction \( \text{CH}_2\text{NH}_2 + \text{O}_3 \rightarrow \) products with a rate constant of \( 7.8(8) \times 10^{-11} \text{ cm}^3 \text{ molecule}^{-1} \text{ s}^{-1} \). So far we have not been able to identify the products, \( \text{O}_2 + \text{CH}_2\text{NH}_2 \) or \( \text{HO}_2 + \text{N}_2\text{C}=\text{NH} \). However, the formation of \( \text{H}_2\text{C}=\text{NH} \) has been proposed as the major channel in the atmospheric oxidation mechanism of methylamine.\(^{15}\)

**Acknowledgements.** Sten Retrup wishes to acknowledge financial support from The Danish Natural Science Research Council and EEC under the TMR Program.

Table 5. Vibrational structure of the \( \pi^* \rightarrow 3p_y \) Rydberg transition.

<table>
<thead>
<tr>
<th>Position/cm(^{-1})</th>
<th>Vib. energy</th>
<th>Assignment</th>
</tr>
</thead>
<tbody>
<tr>
<td>31 300</td>
<td>0</td>
<td>( b(0,0) )</td>
</tr>
<tr>
<td>31 900</td>
<td>600</td>
<td>( b + \nu_1 )</td>
</tr>
<tr>
<td>32 150</td>
<td>850</td>
<td>( b + \nu_2 )</td>
</tr>
<tr>
<td>32 750</td>
<td>1450</td>
<td>( b + \nu_1 + \nu_2 )</td>
</tr>
<tr>
<td>33 000</td>
<td>1700</td>
<td>( b + \nu_3 )</td>
</tr>
<tr>
<td>33 600</td>
<td>2300</td>
<td>( b + \nu_1 + 2\nu_2 )</td>
</tr>
<tr>
<td>33 950</td>
<td>2550</td>
<td>( b + \nu_2 + \nu_3 )</td>
</tr>
<tr>
<td>34 350</td>
<td>3050</td>
<td>( b + \nu_1 + 3\nu_2 )</td>
</tr>
<tr>
<td>34 700</td>
<td>3400</td>
<td>( b + 2\nu_3 )</td>
</tr>
<tr>
<td>35 200</td>
<td>3900</td>
<td>( b + \nu_1 + 4\nu_2 )</td>
</tr>
<tr>
<td>35 550</td>
<td>4250</td>
<td>( b + \nu_2 + 2\nu_3 )</td>
</tr>
<tr>
<td>36 050</td>
<td>4750</td>
<td>( b + \nu_1 + 5\nu_2 )</td>
</tr>
<tr>
<td>36 400</td>
<td>5100</td>
<td>( b + 3\nu_3 )</td>
</tr>
<tr>
<td>36 900</td>
<td>5600</td>
<td>( b + \nu_1 + 6\nu_2 )</td>
</tr>
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</table>

\( \nu_1 = 600 \text{ cm}^{-1} \), \( \nu_2 = 850 \text{ cm}^{-1} \), \( \nu_3 = 1700 \text{ cm}^{-1} \).
The authors thank Dr. R. D. Amos for permission to make use of the CADPAC program package.

References


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