

Vibrational Spectra of the Tris(1,2-ethanediamine)rhodium(III) Cation. I. Normal Coordinate Analysis of the Parent Compound, Three Deuterated, and Four ^{15}N Substituted Species*

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A normal coordinate analysis of the tris(1,2-ethanediamine)-rhodium(III) cation, the $N\text{-}d_{12}$, $C\text{-}d_{12}$ and $N,C\text{-}d_{24}$ deuterated, and the four corresponding ^{15}N substituted species has been accomplished as a 37 body problem (including all atoms). The complex with the three chiral five-membered rings in the more stable δ conformation and the same absolute configuration Λ as in $(+)\text{-}_{589}\text{-}[\text{Co}(\text{en})_3]^{3+}$ was selected for the analysis among the four possible combinations of Λ,Λ absolute configuration with δ,Λ ring conformation; resulting in D_3 symmetry of the complex ion. By fitting 38 force constants in the GVFF (General Valence Force Field) approximation to reproduce more than 500 observed frequencies, the normal modes of vibration for the observed bands can be described in terms of the potential energy distribution (PED) between the symmetry coordinates. The force field and vibrational modes related to the Rh—N bonds and N—Rh—N angles are discussed in some detail.

A large amount of data has been collected on the vibrational spectra of metal chelates of 1,2-ethanediamine (en). However, the interpretation of these results is still very unsatisfactory and band assignments and interpretations are usually made without any assistance from normal coordinate calculations. A partial calculation considering only the nine skeletal atoms was performed by Ashley and Torrible¹ for $\text{Ti}(\text{en})$ tetrahalide complexes and used as a basis for assigning the IR spectrum in the region above 300 cm^{-1} . A more detailed cal-

ulation has been reported by Omura, Nakagawa and Shimanouchi² for the IR active species of several bis(en) metal chelates, but in this case the force constants were refined to fit the frequencies especially in the region below 600 cm^{-1} . Attempts to give detailed assignments of IR and Raman spectra based upon complete normal coordinate calculations have, to our knowledge, not been published.

In the present paper the results of a complete normal coordinate treatment of this ion and seven isotopically labelled species are discussed with special emphasis on the force constants and the vibrational modes involving the central part of the complex compounds. The IR and Raman spectra in the solid state and in solution including polarization measurements of the Raman bands of the parent molecule $[\text{Rh}(\text{en})_3]^{3+}$ and the three deuterated species will be dealt with in separate papers.³ The shifts observed by ^{15}N isotopic substitution are also included here. Hence, this is the first of several papers concerning the vibrational characteristics of the $[\text{Rh}(\text{en})_3]^{3+}$ cation.

STRUCTURE

By investigation of X-ray powder photographs of active racemates it was shown by Andersen *et al.*⁴ that $(+)\text{-}_{589}\text{-}[\text{Co}(\text{en})_3]^{3+}$ and $(-)\text{-}_{589}\text{-}[\text{Rh}(\text{en})_3]^{3+}$ have the same absolute configuration Λ . Since a three-dimensional analysis of $(+)\text{-}_{589}\text{-}[\text{Co}(\text{en})_3]\text{Cl}_3\cdot\text{H}_2\text{O}$ ⁵ revealed the ligand conformation to be δ , i.e. that the

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C-C direction within each chelate ring is approximately parallel to the threefold axis of the complex ion (*lel* arrangement), the same must necessarily be true for the rhodium complex in the solid state. The complex has accordingly the symmetry D_3 with the six nitrogen atoms of the three ligands bonded nearly octahedrally to the central rhodium atom. The present calculations have therefore been based upon a $A-(\delta\delta\delta)$, or $A-lel_3$, model for the $[\text{Rh}(\text{en})_3]^{3+}$ ion.

The Cartesian coordinates were constructed in the following way. The $[\text{Rh}(\text{en})_3]^{3+}$ ion was located in a three-dimensional coordinate system with the rhodium atom *in origo* and with the six nitrogen atoms placed upon the X, Y, and Z axes assuming N-Rh-N angles of 90° . The unknown coordinates were then calculated by a vector analytical method⁶ applied to one of the ligands only. Transcription of (x,y,z) coordinates to the trigonal coordinate system⁶ (x',y',z') proceeded *via* the orthonormal transformations

$$x' = (2/3)^{1/2}z - 6^{-1/2}y - 6^{-1/2}x$$

$$y' = -2^{-1/2}y + 2^{-1/2}x$$

$$z' = 3^{-1/2}z + 3^{-1/2}y + 3^{-1/2}x$$

and finally the coordinates obtained (x',y',z') were rotated $\pm 120^\circ$ around the Z' axis to give the coordinates of the two other ligands.

The average Rh-N distance in (+)-*trans*-1,2-cyclohexanediamine[rhodium(III) nitrate trihydrate] was found⁷ to be 2.08 Å. Since the Rh-N bond length was very close to 1.99 Å in both dimethylglyoxime^{8,9} and ethylenimine¹⁰ complexes, the rounded value of 2.00 Å was adopted in the present calculation. The values used for the ligand distances and bond angles are mostly standard values: $r(\text{N}-\text{H}) = 1.01$ Å, $r(\text{C}-\text{H}) = 1.09$ Å, $r(\text{C}-\text{C}) = 1.53$ Å, $r(\text{C}-\text{N}) = 1.47$ Å, $\angle\text{H}-\text{N}-\text{H} = \angle\text{H}-\text{C}-\text{H} = 111^\circ$, $\angle\text{Rh}-\text{N}-\text{C} = 105^\circ$, $\angle\text{N}-\text{C}-\text{C} = 111^\circ$, $\angle\text{Rh}-\text{N}-\text{H} = 115^\circ$, $\angle\text{N}-\text{C}-\text{H} = 107^\circ$, $\angle\text{Rh}-\text{N}-\text{C}-\text{C} = 33^\circ$.

NORMAL COORDINATE ANALYSIS

The normal coordinate analysis was performed as a 37-body problem using Wilson's GF matrix method as treated in the program of Schachtschneider and Snyder.¹¹ The potential

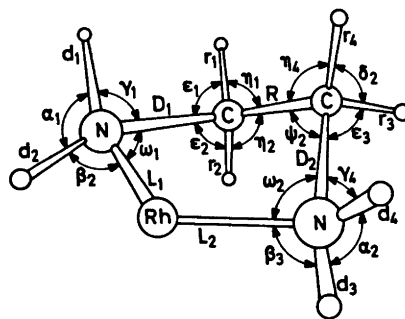


Fig. 1. Internal coordinates of the chelate ring I. Additional coordinates are: Torsion around the Rh-N bonds τ_1 and τ_3 , the N-C bonds π_1 and π_2 , and around the C-C bond Δ . Torsion around the Rh-N bonds (τ_1 and τ_3) have been defined as C-N-Rh-N torsion within a chelate ring. Torsion around the N-C bonds (π_1 and π_2) have been defined as Rh-N-C-N torsion, and around the C-C bond (Δ) as N-C-C-N torsion.

function employed was of the GVFF type originally developed for hydrocarbons,¹² extended to molecules containing the X-CH₂-CH₂-X moiety¹³⁻¹⁶ also present in $[\text{Rh}(\text{en})_3]^{3+}$. The internal coordinates of the chelate ring are shown in Fig. 1, while the internal NRhN deformation coordinates are separately given in Fig. 2. The symmetry coordinates listed in Table 1 were derived making use of the D_3 symmetry of the complex. The redundancies

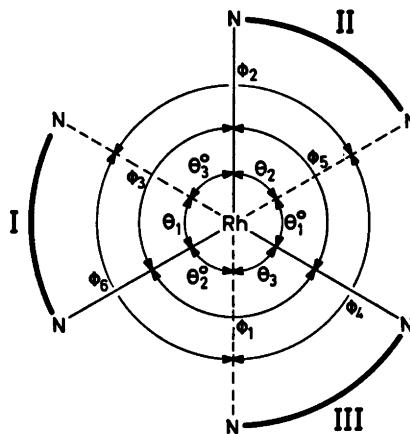


Fig. 2. The internal NRhN deformation coordinates. The numbers I, II, and III refer to the three chelate rings.

Table 1. Symmetry coordinates for the tris(1,2-ethanediamine)Rh(III) cation. The numbers I, II, and III refer to the chelate rings. The symbols used are defined in section (c) of this Table for the chelate ring I and similar expressions are used for the other chelate rings.

(a) Chelate rings

Species A_1

$$S_1 - S_{22} = [Sx(I) + Sx(II) + Sx(III)]/\sqrt{3} \quad (x = a, b, c, d, \dots, v)$$

Species A_2

$$S_1 - S_{20} = [Sx'(I) + Sx'(II) + Sx'(III)]/\sqrt{3} \quad (x = a, b, d, e, \dots, u)$$

Species E

$S_1 = [2Sa(I) - Sa(II) - Sa(III)]/\sqrt{6}$	$S_2 = [Sa'(II) - Sa'(III)]/\sqrt{2}$
$S_3 = [2Sb(I) - Sb(II) - Sb(III)]/\sqrt{6}$	$S_4 = [Sb'(II) - Sb'(III)]/\sqrt{2}$
$S_5 = [2Sc(I) - Sc(II) - Sc(III)]/\sqrt{6}$	
$S_6 = [2Sd(I) - Sd(II) - Sd(III)]/\sqrt{6}$	$S_7 = [Sd'(II) - Sd'(III)]/\sqrt{2}$
$S_8 = [2Se(I) - Se(II) - Se(III)]/\sqrt{6}$	$S_9 = [Se'(II) - Se'(III)]/\sqrt{2}$
$S_{10} = [2Sf(I) - Sf(II) - Sf(III)]/\sqrt{6}$	$S_{11} = [Sf'(II) - Sf'(III)]/\sqrt{2}$
$S_{12} = [2Sg(I) - Sg(II) - Sg(III)]/\sqrt{6}$	$S_{13} = [Sg'(II) - Sg'(III)]/\sqrt{2}$
$S_{14} = [2Sh(I) - Sh(II) - Sh(III)]/\sqrt{6}$	$S_{15} = [Sh'(II) - Sh'(III)]/\sqrt{2}$
$S_{16} = [2Si(I) - Si(II) - Si(III)]/\sqrt{6}$	$S_{17} = [Si'(II) - Si'(III)]/\sqrt{2}$
$S_{18} = [2Sj(I) - Sj(II) - Sj(III)]/\sqrt{6}$	$S_{19} = [Sj'(II) - Sj'(III)]/\sqrt{2}$
$S_{20} = [2Sk(I) - Sk(II) - Sk(III)]/\sqrt{6}$	$S_{21} = [Sk'(II) - Sk'(III)]/\sqrt{2}$
$S_{22} = [2Sl(I) - Sl(II) - Sl(III)]/\sqrt{6}$	$S_{23} = [Sl'(II) - Sl'(III)]/\sqrt{2}$
$S_{24} = [Sm(II) - Sm(III)]/\sqrt{2}$	$S_{25} = [2Sm'(I) - Sm'(II) - Sm'(III)]/\sqrt{6}$
$S_{26} = [2Sn(I) - Sn(II) - Sn(III)]/\sqrt{6}$	$S_{27} = [Sn'(II) - Sn'(III)]/\sqrt{2}$
$S_{28} = [So(II) - So(III)]/\sqrt{2}$	$S_{29} = [2So'(I) - So'(II) - So'(III)]/\sqrt{6}$
$S_{30} = [2Sp(I) - Sp(II) - Sp(III)]/\sqrt{6}$	$S_{31} = [Sp'(II) - Sp'(III)]/\sqrt{2}$
$S_{32} = [Sq(II) - Sq(III)]/\sqrt{2}$	$S_{33} = [2Sq'(I) - Sq'(II) - Sq'(III)]/\sqrt{6}$
$S_{34} = [2Sr(I) - Sr(II) - Sr(III)]/\sqrt{6}$	$S_{35} = [Sr'(II) - Sr'(III)]/\sqrt{2}$
$S_{36} = [Ss(II) - Ss(III)]/\sqrt{2}$	$S_{37} = [2Ss'(I) - Ss'(II) - Ss'(III)]/\sqrt{6}$
$S_{38} = [2St(I) - St(II) - St(III)]/\sqrt{6}$	$S_{39} = [St'(II) - St'(III)]/\sqrt{2}$
$S_{40} = [2Su(I) - Su(II) - Su(III)]/\sqrt{6}$	$S_{41} = [Su'(II) - Su'(III)]/\sqrt{2}$
$S_{42} = [2Sv(I) - Sv(II) - Sv(III)]/\sqrt{6}$	

(b) Symmetry coordinates involving NRhN deformation (δ NRhN)Species A_1

$$S_{23} = [\phi_1 + \phi_2 + \phi_3 + \phi_4 + \phi_5 + \phi_6]/\sqrt{6}$$

$$S_{24} = [\theta_1 + \theta_2 + \theta_3 + \theta_1^\circ + \theta_2^\circ + \theta_3^\circ]/\sqrt{6}$$

$$S_{25} = [\theta_1 + \theta_2 + \theta_3 - \theta_1^\circ - \theta_2^\circ - \theta_3^\circ]/\sqrt{6}$$

Species A_2

$$S_{21} = [\phi_1 - \phi_2 + \phi_3 - \phi_4 + \phi_5 - \phi_6]/\sqrt{6}$$

Species E

$$S_{43} = [2\phi_1 + 2\phi_2 - \phi_3 - \phi_4 - \phi_5 - \phi_6]/\sqrt{12}$$

$$S_{44} = [\phi_3 - \phi_4 + \phi_5 - \phi_6]/2$$

$$S_{45} = [2\theta_1 - \theta_2 - \theta_3 + 2\theta_1^\circ - \theta_2^\circ - \theta_3^\circ]/\sqrt{12}$$

$$S_{46} = [\theta_2 - \theta_3 + \theta_2^\circ - \theta_3^\circ]/2$$

Table 1. Continued.

(c) Local symmetry coordinates of the chelate ring I

Symmetry coordinate	Symbol	Description
$Sa(I) = (L_1 + L_2)/\sqrt{2}$	$\nu_s \text{RhN}$	Symm. RhN stretch
$Sa'(I) = (L_1 - L_2)/\sqrt{2}$	$\nu_{as} \text{RhN}$	Asym. RhN stretch
$Sb(I) = (D_1 + D_2)/\sqrt{2}$	$\nu_s \text{CN}$	Symm. CN stretch
$Sb'(I) = (D_1 - D_2)/\sqrt{2}$	$\nu_{as} \text{CN}$	Asymm. CN stretch
$Sc(I) = R$	ν_{CC}	CC stretch
$Sd(I) = (d_1 + d_2 + d_3 + d_4)/2$	$\nu_s \text{NH}$	Symm. NH stretch
$Sd'(I) = (d_1 + d_2 - d_3 - d_4)/2$	$\nu_s \text{NH}$	Symm. NH stretch
$Se(I) = (d_1 - d_2 + d_3 - d_4)/2$	$\nu_{as} \text{NH}$	Asym. NH stretch
$Se'(I) = (d_1 - d_2 - d_3 + d_4)/2$	$\nu_{as} \text{NH}$	Asym. NH stretch
$Sf(I) = (r_1 + r_2 + r_3 + r_4)/2$	$\nu_s \text{CH}$	Symm. CH stretch
$Sf'(I) = (r_1 + r_2 - r_3 - r_4)/2$	$\nu_s \text{CH}$	Symm. CH stretch
$Sg(I) = (r_1 - r_2 + r_3 - r_4)/2$	$\nu_{as} \text{CH}$	Asym. CH stretch
$Sg'(I) = (r_1 - r_2 - r_3 + r_4)/2$	$\nu_{as} \text{CH}$	Asym. CH stretch
$Sh(I) = (\omega_1 + \omega_2)/\sqrt{2}$	$\delta_s \text{RhNC}$	Symm. RhNC deformation
$Sh'(I) = (\omega_1 - \omega_2)/\sqrt{2}$	$\delta_{as} \text{RhNC}$	Asym. RhNC deformation
$Si(I) = (\psi_1 + \psi_2)/\sqrt{2}$	$\delta_s \text{NCC}$	Symm. NCC deformation
$Si'(I) = (\psi_1 - \psi_2)/\sqrt{2}$	$\delta_{as} \text{NCC}$	Asym. NCC deformation
$Sj(I) = (\alpha_1 + \alpha_2)/\sqrt{2}$	δNH_2	NH_2 deformation
$Sj'(I) = (\alpha_1 - \alpha_2)/\sqrt{2}$	δNH_2	NH_2 deformation
$Sk(I) = (\delta_1 + \delta_2)/\sqrt{2}$	δCH_2	CH_2 deformation
$Sk'(I) = (\delta_1 - \delta_2)/\sqrt{2}$	δCH_2	CH_2 deformation
$Sl(I) = (\beta_1 + \beta_2 + \beta_3 + \beta_4)/2$	$[Sl(I) + Sn(I)]/\sqrt{2} = \delta \text{NH}_2$	NH_2 deformation
$Sl'(I) = (\beta_1 + \beta_2 - \beta_3 - \beta_4)/2$	$[Sl'(I) + Sn'(I)]/\sqrt{2} = \delta \text{NH}_2$	NH_2 deformation
$Sm(I) = (\beta_1 - \beta_2 + \beta_3 - \beta_4)/2$	$[Sm(I) + So(I)]/\sqrt{2} = \rho \text{NH}_2$	NH_2 rock
$Sm'(I) = (\beta_1 - \beta_2 - \beta_3 + \beta_4)/2$	$[Sm'(I) + So'(I)]/\sqrt{2} = \rho \text{NH}_2$	NH_2 rock
$Sn(I) = (\gamma_1 + \gamma_2 + \gamma_3 + \gamma_4)/2$	$[Sl(I) - Sn(I)]/\sqrt{2} = \omega \text{NH}_2$	NH_2 wag
$Sn'(I) = (\gamma_1 + \gamma_2 - \gamma_3 - \gamma_4)/2$	$[Sl'(I) - Sn'(I)]/\sqrt{2} = \omega \text{NH}_2$	NH_2 wag
$So(I) = (\gamma_1 - \gamma_2 + \gamma_3 - \gamma_4)/2$	$[Sm(I) - So(I)]/\sqrt{2} = t \text{NH}_2$	NH_2 twist
$So'(I) = (\gamma_1 - \gamma_2 - \gamma_3 + \gamma_4)/2$	$[Sm'(I) - So'(I)]/\sqrt{2} = t \text{NH}_2$	NH_2 twist
$Sp(I) = (\epsilon_1 + \epsilon_2 + \epsilon_3 + \epsilon_4)/2$	$[Sp(I) + Sr(I)]/\sqrt{2} = \delta \text{CH}_2$	CH_2 deformation
$Sp'(I) = (\epsilon_1 + \epsilon_2 - \epsilon_3 - \epsilon_4)/2$	$[Sp'(I) + Sr'(I)]/\sqrt{2} = \delta \text{CH}_2$	CH_2 deformation
$Sq(I) = (\epsilon_1 - \epsilon_2 + \epsilon_3 - \epsilon_4)/2$	$[Sq(I) + Ss(I)]/\sqrt{2} = \rho \text{CH}_2$	CH_2 rock
$Sq'(I) = (\epsilon_1 - \epsilon_2 - \epsilon_3 + \epsilon_4)/2$	$[Sq'(I) + Ss'(I)]/\sqrt{2} = \rho \text{CH}_2$	CH_2 rock
$Sr(I) = (\eta_1 + \eta_2 + \eta_3 + \eta_4)/2$	$[Sp(I) - Sr(I)]/\sqrt{2} = \omega \text{CH}_2$	CH_2 wag
$Sr'(I) = (\eta_1 + \eta_2 - \eta_3 - \eta_4)/2$	$[Sp'(I) - Sr'(I)]/\sqrt{2} = \omega \text{CH}_2$	CH_2 wag
$Ss(I) = (\eta_1 - \eta_2 + \eta_3 - \eta_4)/2$	$[Sq(I) - Ss(I)]/\sqrt{2} = t \text{CH}_2$	CH_2 twist
$Ss'(I) = (\eta_1 - \eta_2 - \eta_3 + \eta_4)/2$	$[Sq'(I) - Ss'(I)]/\sqrt{2} = t \text{CH}_2$	CH_2 twist
$St(I) = (\tau_1 + \tau_2)/\sqrt{2}$	$\tau_s \text{RhN}$	Symm. RhN torsion
$St'(I) = (\tau_1 - \tau_2)/\sqrt{2}$	$\tau_{as} \text{RhN}$	Asym. RhN torsion
$Su(I) = (\pi_1 + \pi_2)/\sqrt{2}$	$\tau_s \text{NC}$	Symm. NC torsion
$Su'(I) = (\pi_1 - \pi_2)/\sqrt{2}$	$\tau_{as} \text{NC}$	Asym. NC torsion
$Sv(I) = \Delta$	τ_{cc}	CC torsion

Table 2. Valence force constants for the [Rh(en)₃]³⁺ cation.

Force type	Constants symbol	Group	Coordinate(s) involved	Atoms common to interacting coordinates	Value ^a Initial	Final
Stretch	K_r	CH ₂	C-H	-	4.55 ^b	4.706
	K_d	NH ₂	N-H	-	6.42 ^c	5.669
	K_R	CH ₂ -CH ₂	C-C	-	4.39 ^b	3.581
	K_D	CH ₂ -NH ₂	C-N	-	4.97 ^c	4.692
Stretch-stretch	K'_L	RhN ₆	Rh-N	-	2.31 ^d	1.607
	F_r	CH ₂	C-H, C-H	C	0.01 ^b	0.0398
	F_d	NH ₂	N-H, N-H	N	0 ^c	0.0307
	F_{RD}	CH ₂ -CH ₂ -NH ₂	C-C, C-N	C	0.10 ^b	0.391
Bend	F'_{LL}	RhN ₆	Rh-N, Rh-N, <i>cis</i>	Rh	0.05 ^d	0.250
	F'_{LL}	RhN ₆	Rh-N, Rh-N, <i>trans</i>	Rh	-	-0.0868
	H_δ	CH ₂	<HCH	-	0.55 ^b	0.554
	H_α	NH ₂	<HNH	-	0.64 ^c	0.547
	H_η	CH ₂ -CH ₂	<HCC	-	0.656 ^b	0.651
	H_ϵ	CH ₂ -NH ₂	<HCN	-	0.656 ^b	0.732
	H_γ	CH ₂ -NH ₂	<CNH	-	0.578 ^c	0.692
	H_ψ	CH ₂ -CH ₂ -NH ₂	<CCN	-	1.13 ^b	1.087
	H_β	Rh-NH ₂	<HNRh	-	0.19 ^e	0.458
	H_ω	Rh-NH ₂ -CH ₂	<RhNC	-	0.77 ^f	0.755
	$H_\phi = H_\theta$	RhN ₆	<NRhN	-	0.20 ^f	1.100
	Stretch bend	$F_{R\eta}$	CH ₂ -CH ₂	C-C, <HCC	C-C	0.328 ^b
$F_{R\epsilon}$		CH ₂ -CH ₂ -NH ₂	C-C, <HCN	C	0.079 ^b	0.101
$F_{R\psi}$		CH ₂ -CH ₂ -NH ₂	C-C, <CCN	C-C	0.42 ^b	0.250
$F_{D\epsilon}$		CH ₂ -NH ₂	C-N, <HCN	C-N	0.36 ^c	0.473
$F_{D\gamma}$		CH ₂ -NH ₂	C-N, <HNC	C-N	0.16 ^c	0.385
$F_{D\eta}$		CH ₂ -CH ₂ -NH ₂	C-N, <HCC	C	-	0.141
$F_{D\psi}$		CH ₂ -CH ₂ -NH ₂	C-N, <CCN	C-N	0.42 ^b	0.466
$F_{L\omega}$		Rh-NH ₂ -CH ₂	Rh-N, <RhNC	Rh-N	-	0.216
$F_{D\omega}$		Rh-NH ₂ -CH ₂	C-N, <RhNC	C-N	-	0.0984
Bend-bend		F_η	CH ₂ -C	<HCC, <HCC	C-C	-0.021 ^b
	F_ϵ	CH ₂ -N	<HCN, <HCN	C-N	-0.031 ^c	-0.0218
	F_γ	NH ₂ -C	<HNC, <HNC	C-N	-0.05 ^c	-0.128
	F_β	NH ₂ -Rh	<HNRh, <HNRh	N-Rh	-	0.0856
	$F_\phi = F_\theta$	RhN ₆	<NRhN, <NRhN	Rh-N	-	-0.200
	$F'_\phi = F'_\theta$	RhN ₆	<NRhN, <NRhN coplanar	Rh-N	-	0.200
Torsion	f_η^t	CH ₂ -CH ₂	<HCC, <CCH	C-C	0.127 ^b	0.0996
	H_t	RhN ₆	Rh-N	-	-	0.205
	H_π	CH ₂ -NH ₂	C-N	-	0.058 ^c	0.060
	H_Δ	CH ₂ -CH ₂	C-C	-	0.058 ^c	0.127

^a In units of m dyn/Å (stretch constants) m dyn/rad (stretch-bend interaction constants) and m dyn Å/(rad)² (bending and torsion constants). ^b Refs. 12 and 17. ^c Ref. 18. ^d Ref. 19. ^e Ref. 2. ^f Ref. 20.

7A₁+4A₂+11E included here were in the calculations eliminated directly by the program. The initial force constants, based on values for similar molecules^{12,17-20} are listed in Table 2 for comparison with the final GVF constants. The calculated frequencies are given in Table 3, which also includes an approximate description of the vibrational modes based upon the PED (potential energy distribution) of each vibration among the symmetry coordinates. The PED

among the force constants, $K_h J_{\lambda h} / \lambda^{11}$ was also calculated to estimate the significant force constants for each vibration, but are not listed in order to save space.

Treatment of [Rh(en)₃]³⁺ under the point group D₃ reduces the 105 normal modes of vibration to the irreducible representation $\Gamma = 18A_1(\text{R}) + 17A_2(\text{IR}) + 35E(\text{R,IR})$, where (R) and (IR) indicate the Raman and infrared active modes, respectively. The eight isotopic

species considered here accordingly give us potentially 144 A_1 , 136 A_2 , and 280 E frequencies, or a total of 560 frequencies which we have tried to fit to the minimum number of force constants in an internally consistent approximation.

Method of calculation. Since the experimental Raman data included semiquantitative depolarization ratios for many bands, it was decided to perform exploratory calculations of the A_1 block separately and obtain a fit of the calculated frequencies to those of the polarized Raman bands. The force field obtained was then transferred to species A_2 and E after having properly utilized the molecular symmetry, and a provisional assignment of approximately one half of the 560 fundamentals made. Least squares refinements of each species separately disclosed the presence of inconsistencies which led to the introduction of new interaction force constants and revision of the assigned fundamentals. An examination of the Jacobian elements indicated that several of these were very poorly determined while others were essential to insure satisfactory convergence. The following constraints were now made to the calculations. (i) The force constants were not allowed to deviate beyond some fixed limits found valid for similar molecules (*vide infra*). (ii) The final force field should as far as possible be truly convergent, *i.e.* obtained by allowing all force constants to vary simultaneously. (iii) The standard error (excluding NH/ND and CH/CD stretching) for each species (A_1, A_2, E) in any of the four isotopic molecules should not exceed a fixed limit (1 % intended). (iv) The number of force constants should be held as low as possible. With these constraints it was possible to assign almost all fundamentals and explain the significant bands in the observed spectra, by using a 38-parameter GVFF.

Force field related to RhN_6 . The approach developed here is based mainly upon the general considerations by Claassen²¹ to molecules of formula XY_6 and the results for hexamine complexes derived from Ru, Rh, Ir, and Os¹⁹ and Ni.²² The vibrations involving Rh–N stretching could only be fitted satisfactorily by including the three force constants K_L (Rh–N stretching), F_{LL} (bond with a bond at right angles to it), and F'_{LL} (bond with opposite

bond). No improvement was obtained by introducing different interaction force constants F_{LL} for interactions within a chelate ring and interaction between Rh–N bonds of two different chelate rings. The interaction force constants $F_{L\phi}$ and $F_{L\theta}$ were found to be small and omitted in the final calculations.

The force constants for N–Rh–N deformation were initially introduced with different values for deformation within a chelate ring and deformation between two rings. This was considered important since all equilibrium values for N–Rh–N angles were put equal to 90° which is a reasonable but nevertheless conjectural value, being at variance with an $A-(\lambda, \lambda, \lambda)$ (ob_3) isomer⁷ of the $[Rh(-chxn)_3]^{3+}$ cation. However, as the calculations proceeded it became clear that this distinction was not warranted and accordingly the constraint that all $H_\theta = H_\phi$ was introduced. To be consistent the interaction constants were constrained in the same way, *i.e.* all interactions involving deformation of the RhN_6 part of the chelate were considered equal whether the deformation occurs within a chelate ring or between two chelate rings. The force constants H_θ , F_θ , and F'_θ were now determined by trial and error. These constraints ensured convergence of the remaining force field (*vide supra*). The standard error of the final set did not exceed 1.1 % for each species (A_1, A_2, E) in any of the eight compounds.

The description of the low frequency modes in terms of PED on symmetry coordinates were not sufficient for an understanding of the vibrational spectrum of $[Rh(en)_3]^{3+}$ in this region. Accordingly, we finally calculated the elements of the transformation matrix L_x between the Cartesian displacement vector X and the normal coordinate vector Q .

RESULTS AND DISCUSSION

Some features considered to be of general interest will be pointed out from the results of the normal coordinate analysis. Nevertheless, in the following discussion it should be kept in mind that (i) the experimental frequencies used are not unambiguously classified to their species from the Raman polarization ratios and (ii) certain constraints have been imposed on the force field. Undoubtedly, these sources

of error are only partly counterbalanced by attempting alternative assignments of fundamentals in all cases of reasonable doubt and systematic attempts to evaluate the significance of the force field during the calculations as discussed above.

Potential constants. Let us compare the values of the initial and the final valence force constants listed in the last two columns of Table 2. The agreement is very satisfactory for force constants related to the ethylenediamine ligand provided allowance is made for the somewhat larger variation observed for interaction force constants than for pure stretch and bending constants. Appreciable changes are noted for some of the force constants involving the amino groups (*e.g.* K_d, H_α and F_γ), but this is easily understandable as a result of the coordination to Rh. The changes in K_R and K_D are mainly the result of the increase in K_{RD} following complex formation. From the overall pattern we may conclude this part of the force field to be essentially comparable to that of similar molecules.

Very similar changes have been observed for the Urey-Bradley force constants of bis(en) metal chelates³ compared with those found for unchelated aliphatic amines.¹⁰ Thus, for example, the value of the N-H stretching force constant was found to decrease from 6.3 mdyn/Å in amines to *ca.* 5.7 mdyn/Å in chelated 1,2-ethanediamine. In the GVFF developed here, K_D decreased from 6.42 mdyn/Å in aliphatic amines to 5.669 mdyn/Å in $[\text{Rh}(\text{en})_3]^{3+}$ in complete harmony. This behaviour is hardly coincidental but rather reflects a mutual consistency between the present and previous calculations.

An evaluation of the force field related to the central part of the $[\text{Rh}(\text{en})_3]^{3+}$ ion is much more difficult, since data suitable for comparison have not been reported. The differences between initial and final GVF constants (Table 2) for the RhN_6 group are therefore largely due to an unprecedented choice of the initial value rather than real discrepancies. From an assignment of five fundamentals for $[\text{Rh}(\text{NH}_3)_6]\text{Cl}_3$ in the low frequency region, assuming O_h symmetry and treating the NH_3 molecules as single masses, Griffith¹⁹ calculated the force constant for Rh-N stretch, K_L , to be 2.3–2.5 mdyn/Å and the interaction force

constant for two Rh-N *cis* bonds, F'_{LL} , to be 0.05 mdyn/Å. We have attempted to evaluate the force field in more detail using the GVF expressions given by Claassen²¹ with suitable approximations, but the derived force constants have in many cases complex solutions and are very dependent on the details of the sophistication. Such calculations have been successfully carried out by Müller *et al.*²² for the $[\text{Ni}(\text{NH}_3)_6]^{2+}$ ion indicating values of 0.87, 0.12, and 0.00–0.01 mdyn/Å for Ni-N stretch, *cis* Ni-N and *trans* Ni-N stretch-stretch interactions, respectively. The values obtained here for K_L , K_{LL} , and F'_{LL} of 1.607, 0.250, and –0.0868 mdyn/Å are considered quite reliable since they depend heavily upon the assignment of the fundamentals involving Rh-N stretching which in fact are some of those most reliable in the experimental material (*cf.* Schmidt and Müller²³).

From these results we conclude that K_L decreases somewhat from $[\text{Rh}(\text{NH}_3)_6]^{3+}$ to $[\text{Rh}(\text{en})_3]^{3+}$ but this trend does not necessarily reflect a weaker bond in the latter compound but may be due to an erroneous choice of the Rh-N bond length in our calculations. The value of F'_{LL} appears to increase to the fivefold value on changing the ligand from NH_3 to 1,2-ethanediamine, but if we consider instead the ratio K_L/F'_{LL} it compares favourably with $[\text{Ni}(\text{NH}_3)_6]^{2+}$. In short, the values are not unreasonable, but unsatisfactory for deductions regarding the detailed nature of the bonds in the complex.

The GVF constant for N-Rh-N deformation was found to be 1.10 mdyn Å/(rad)², considerably higher than the corresponding values for $[\text{Ni}(\text{NH}_3)_6]^{2+}$ ²² and for dimethylglyoxime chelates¹⁹ which are in the range 0.10–0.30 mdyn Å/(rad)². However, in the UBFF approximation the appropriate range for 1,2-ethanediamine chelates is 0.16–0.40 mdyn/Å (in-plane bending) and 0.53–0.90 mdyn Å (out-of-plane bending)³ suggesting the value obtained here to be significant. The numerical values of the interaction force constants F_ϕ and F'_ϕ and of the force constant for Rh-N torsion are also considerably higher than expected from other complex compounds²² and suggest a considerable stiffening of $[\text{Rh}(\text{en})_3]^{3+}$. The high values of the bending force constants H_β and H_ω and of the interaction

Table 3. Calculated (ν_{calc} ; cm^{-1}) and observed (ν_{obs} ; cm^{-1}) fundamentals and main potential energy distribution (PED, %) for $[\text{Rh}(\text{en})_2]^{3+}$ from a 38-parameter GVFF based upon the spectra of $[\text{Rh}(\text{en})_2]\text{Cl}_3$ and 7 isotopic species.^a

Species and No.	$[\text{Rh}(\text{en})_2]^{3+}$		^{15}N shift ^d		PED ^e		$\text{N}-d_{12}[\text{Rh}(\text{en})_2]^{3+}$		^{15}N shift ^d		$\text{C}-d_{13}[\text{Rh}(\text{en})_2]^{3+}$		$\text{N}, \text{C}-d_{24}[\text{Rh}(\text{en})_2]^{3+}$								
	ν_{calc}	ν_{obs}	ν_{calc}	ν_{obs}	calc	obs	No.	ν_{calc}	ν_{obs}	calc	obs	No.	ν_{calc}	ν_{obs}	calc	obs					
A ₁	ν_1	3235	3245	10	10	$\nu_{\text{as}}\text{NH}(100)$	ν_3	2398	2397	14	10	ν_1	3235	3245	10	0	ν_1	2399	2391	15	8
	ν_2	3175	3150	6		$\nu_{\text{s}}\text{NH}(100)$	ν_4	2306	2339	9	10	ν_2	3175	3192	6	8	ν_2	2306	2330	9	5
	ν_3	2973	2968	0	6	$\nu_{\text{as}}\text{CH}(99)$	ν_1	2973	2972	0	10	ν_3	2234	2238	0	4	ν_3	2233	2137	0	2
	ν_4	2911	2906	0	5	$\nu_{\text{s}}\text{CH}(99)$	ν_2	2911	2907	0	10	ν_4	2128	2155	0	3	ν_4	2128	2137	0	1
	ν_5	1609	1607	5	3	$\delta\text{NH}_2(97)$	ν_8	1189	1187	6	10	ν_5	1609	1605	5	3	ν_5	1208	1202	8	10
	ν_6	1473	1469	0	2	$\delta\text{CH}_2(100)$	ν_5	1472	1469	0	3	ν_6	1089	1069	3	3	ν_6	1085	1090	1	0
	ν_7	1373	1375	2	0	$\omega\text{CH}_2(73)$	ν_6	1352	1353	1	3	ν_{10}	967	950	3	3	ν_{11}	846	838	1	1
	ν_8	1327	1332	1	3	$\omega\text{CH}_2(62), \text{tNH}_2(32)$	ν_7	1318	1307	2	0	ν_{11}	927	925	8	15	ν_{10}	925	929	4	4
	ν_9	1297	1292	3	3	$\text{tNH}_2(46), \text{tCH}_2(37)$	ν_{12}	845	844	0	2	ν_6	1309	1315	3	0	ν_9	1000	1002	11	12
	ν_{10}	1183	1182	2	3	$\omega\text{NH}_2(72)$	ν_{11}	976	970	11	10	ν_7	1258	1258	3	6	ν_8	1039	1048	10	8
	ν_{11}	1059	1061	14	10	$\nu\text{CN}(80), \nu\text{CC}(13)$	ν_{10}	1055	1057	10	10	ν_8	1110	1103	8	2	ν_6	1168	1169	2	9
	ν_{12}	996	1007	3	6	$\rho\text{CH}_2(53), \nu\text{CC}(16)$	ν_9	1106	1106	3	6	ν_{12}	882	892	5	5	ν_{12}	783	780	0	0
	ν_{13}	871	883	4	6	$\nu\text{CC}(49), \nu\text{CN}(20)$	ν_{13}	790	808	0	3	ν_{13}	773	771	2	4	ν_{13}	741	751	1	1
	ν_{14}	749	750	4	4	$\rho\text{NH}_2(87)$	ν_{14}	592	587	6	5	ν_{14}	716	719	2	0	ν_{14}	578	570	6	7
	ν_{15}	547	545	14	12	$\nu_2\text{Rhn}(68)$	ν_{15}	504	512	12	14	ν_{15}	543	536	14	14	ν_{15}	499	502	10	8
	ν_{16}	308	315	5	7	$\delta\text{NRhn}(31), \delta_{\text{as}}\text{NCC}(19), \tau\text{CC}(15)$	ν_{16}	278	273	2	2	ν_{16}	287	285	5	8	ν_{16}	266	260	3	2
	ν_{17}	272	272	3	0	$\delta\text{NRhn}(36), \delta_{\text{s}}\text{RhNC}(27), \nu_2\text{Rhn}(12)$	ν_{17}	259	268	2	3	ν_{17}	256	260	3	5	ν_{17}	237	244	3	3
ν_{18}	200	195	2	2	$\delta\text{NRhn}(62), \tau\text{CC}(13)$	ν_{18}	191	183	2	3	ν_{18}	173	170	1	3	ν_{18}	170	170	1	1	
A ₂	ν_{19}	3235	3230	10	30	$\nu_{\text{as}}\text{NH}(100)$	ν_{21}	2397	2397	14	10	ν_{19}	3234	3210	10	10	ν_{19}	2397	2390	14	15
	ν_{20}	3174	3145	5		$\nu_{\text{s}}\text{NH}(100)$	ν_{22}	2303	2379	7	8	ν_{20}	3174	3170	6	8	ν_{20}	2303	2290	7	4
	ν_{21}	2966	2964	0		$\nu_{\text{as}}\text{CH}(99)$	ν_{19}	2966	2966	0	0	ν_{21}	2214	2225	0	0	ν_{21}	2213	2196	0	0
	ν_{22}	2909	2890	0		$\nu_{\text{s}}\text{CH}(99)$	ν_{20}	2909	2905	0	0	ν_{22}	2124	2135	0	0	ν_{22}	2124	2132	0	0
	ν_{23}	1607	1607	5	3	$\delta\text{NH}_2(97)$	ν_{23}	1184	1187	6	10	ν_{23}	1606	1605	5	4	ν_{23}	1192	1190	8	10
	ν_{24}	1460	1459	0		$\delta\text{CH}_2(98)$	ν_{24}	1459	1466	1	0	ν_{24}	1065	1066	0	0	ν_{24}	1075	1080	1	1
	ν_{25}	1334	1330	1	3	$\omega\text{CH}_2(65), \text{tNH}_2(21)$	ν_{25}	1305	1307	1	0	ν_{27}	889	890	5	5	ν_{25}	1115	1113	4	3
	ν_{26}	1300	1305	3	5	$\text{tNH}_2(46), \text{tCH}_2(37)$	ν_{26}	945	956	2	10	ν_{28}	1287	1290	2	2	ν_{27}	968	971	8	8
	ν_{27}	1217	1217	0		$\text{tCH}_2(59), \text{tNH}_2(32)$	ν_{28}	1254	1270	2	4	ν_{28}	922	922	4	6	ν_{28}	863	824	0	7
	ν_{28}	1170	1163	4	1	$\omega\text{NH}_2(84)$	ν_{29}	879	888	2	0	ν_{29}	1230	1229	3	4	ν_{29}	808	824	0	7
	ν_{29}	1031	1028	11	8	$\nu\text{CN}(81)$	ν_{27}	1039	1038	15	18	ν_{26}	1093	1088	10	4	ν_{28}	993	1004	10	12
	ν_{30}	816	812	4	4	$\rho\text{CH}_2(59), \rho\text{NH}_2(26)$	ν_{30}	791	795	4	5	ν_{31}	693	694	6	4	ν_{28}	682	673	6	6
	ν_{31}	779	785	7	6	$\rho\text{NH}_2(58), \rho\text{CH}_2(11)$	ν_{31}	655	650	7	7	ν_{30}	769	785	5	5	ν_{31}	627	628	5	10
ν_{32}	592	580	5	6	$\delta_{\text{as}}\text{NCC}(35), \delta_{\text{as}}\text{RhNC}(15), \rho\text{CH}_2(22)$	ν_{32}	532	539	3	4	ν_{32}	510	511	3	3	ν_{32}	468	480	3	3	
ν_{33}	441	445	6	4	$\nu_{\text{as}}\text{RhN}(84)$	ν_{33}	423	431	4	4	ν_{33}	426	417	4	4	ν_{33}	413	413	4	4	
ν_{34}	253	240	4	4	$\tau\text{Rhn}(41), \delta\text{NRhn}(39)$	ν_{34}	222	226	2	0	ν_{34}	242	242	3	0	ν_{34}	216	220	3	0	
ν_{35}	111	110	1	1	$\delta\text{NRhn}(55), \tau\text{Rhn}(34)$	ν_{35}	107	113	0	0	ν_{35}	102	106	0	0	ν_{35}	99	94	0	0	

Table 3. Continued.

<i>E</i>	<i>ν</i> ₃₆	3232	3245	10	10	<i>ν</i> _{as} NH(100)	<i>ν</i> ₄₀	2390	2397	14	10	<i>ν</i> ₃₈	3232	3245	10	10	<i>ν</i> ₃₆	2390	2391	14	8
	<i>ν</i> ₃₇	3230	3230	10	30	<i>ν</i> _{as} NH(100)	<i>ν</i> ₄₁	2387	2397	14	10	<i>ν</i> ₃₇	3230	3210	10	10	<i>ν</i> ₃₇	2387	2390	14	15
	<i>ν</i> ₃₈	3174	3150	5	5	<i>ν</i> _s NH(100)	<i>ν</i> ₄₃	2304	2339	8	10	<i>ν</i> ₃₈	3174	3192	5	8	<i>ν</i> ₃₈	2304	2330	8	5
	<i>ν</i> ₃₉	3173	3145	5	5	<i>ν</i> _s NH(100)	<i>ν</i> ₄₃	2302	2279	8	8	<i>ν</i> ₃₉	3173	3170	5	8	<i>ν</i> ₃₉	2302	2290	8	7
	<i>ν</i> ₄₀	2971	2968	0	10	<i>ν</i> _{as} CH(99)	<i>ν</i> ₃₆	2971	2972	0	6	<i>ν</i> ₄₀	2971	2943	0	1	<i>ν</i> ₄₀	2925	2255	0	0
	<i>ν</i> ₄₁	2966	2964	0	0	<i>ν</i> _{as} CH(99)	<i>ν</i> ₃₇	2966	2966	0	4	<i>ν</i> ₄₁	2212	2225	0	0	<i>ν</i> ₄₁	2211	2196	0	0
	<i>ν</i> ₄₂	2911	2906	0	5	<i>ν</i> _s CH(99)	<i>ν</i> ₃₈	2911	2907	0	2	<i>ν</i> ₄₂	2127	2135	0	0	<i>ν</i> ₄₂	2127	2132	0	0
	<i>ν</i> ₄₃	2909	2890	0	0	<i>ν</i> _s CH(99)	<i>ν</i> ₃₉	2909	2905	0	8	<i>ν</i> ₄₃	2123	2135	0	0	<i>ν</i> ₄₃	2123	2132	0	0
	<i>ν</i> ₄₄	1606	1607	5	3	<i>δ</i> NH ₃ (99)	<i>ν</i> ₅₀	1185	1187	7	10	<i>ν</i> ₄₄	1606	1605	5	3	<i>ν</i> ₄₄	1196	1190	7	10
	<i>ν</i> ₄₅	1604	1607	5	3	<i>δ</i> NH ₃ (99)	<i>ν</i> ₅₁	1181	1187	6	10	<i>ν</i> ₄₅	1604	1605	5	3	<i>ν</i> ₄₅	1183	1190	6	10
	<i>ν</i> ₄₆	1478	1469	0	2	<i>δ</i> CH ₃ (94)	<i>ν</i> ₄₄	1478	1474	0	3	<i>ν</i> ₄₆	1066	1066	0	0	<i>ν</i> ₄₆	1074	1077	1	1
	<i>ν</i> ₄₇	1464	1459	1	1	<i>δ</i> CH ₃ (96)	<i>ν</i> ₄₅	1464	1467	1	1	<i>ν</i> ₄₇	1057	1068	5	5	<i>ν</i> ₄₇	1066	1069	0	0
	<i>ν</i> ₄₈	1380	1374	1	2	<i>ν</i> CH ₃ (56), <i>ν</i> CH ₃ (31)	<i>ν</i> ₄₆	1375	1385	1	1	<i>ν</i> ₄₈	988	980	3	0	<i>ν</i> ₄₈	1004	1003	6	12
	<i>ν</i> ₄₉	1355	1357	1	1	<i>ν</i> CH ₃ (69), <i>ν</i> CH ₃ (13)	<i>ν</i> ₄₇	1338	1352	2	2	<i>ν</i> ₄₉	957	950	8	0	<i>ν</i> ₄₉	843	838	1	1
	<i>ν</i> ₅₀	1318	1310	0	5	<i>ν</i> CH ₃ (47), <i>ν</i> CH ₃ (38)	<i>ν</i> ₄₈	1305	1307	0	0	<i>ν</i> ₅₀	935	927	4	7	<i>ν</i> ₅₀	1155	1150	2	7
	<i>ν</i> ₅₁	1303	1305	3	5	<i>ν</i> NH ₃ (65), <i>ν</i> CH ₃ (22)	<i>ν</i> ₅₂	1064	1058	4	4	<i>ν</i> ₅₁	1286	1288	2	3	<i>ν</i> ₅₁	993	1003	3	12
	<i>ν</i> ₅₂	1296	1293	3	4	<i>ν</i> NH ₃ (88)	<i>ν</i> ₅₆	959	962	5	8	<i>ν</i> ₅₂	1283	1277	2	1	<i>ν</i> ₅₂	894	893	1	0
	<i>ν</i> ₅₃	1242	1227	1	1	<i>ν</i> CH ₃ (54), <i>ν</i> NH ₃ (33)	<i>ν</i> ₄₉	1256	1270	1	4	<i>ν</i> ₅₃	841	845	4	4	<i>ν</i> ₅₃	788	790	0	0
	<i>ν</i> ₅₄	1181	1173	2	2	<i>ν</i> NH ₃ (77), <i>ν</i> CH ₃ (14)	<i>ν</i> ₅₅	979	980	9	8	<i>ν</i> ₅₄	1261	1256	3	2	<i>ν</i> ₅₄	959	929	4	4
	<i>ν</i> ₅₅	1167	1163	4	1	<i>ν</i> NH ₃ (80), <i>ν</i> CH ₃ (14)	<i>ν</i> ₅₇	882	888	2	0	<i>ν</i> ₅₅	1227	1226	3	3	<i>ν</i> ₅₅	978	980	13	15
	<i>ν</i> ₅₆	1065	1059	17	11	<i>ν</i> CN(92)	<i>ν</i> ₅₃	1062	1051	14	7	<i>ν</i> ₅₆	1117	1133	7	5	<i>ν</i> ₅₆	818	828	1	11
	<i>ν</i> ₅₇	1028	1028	13	8	<i>ν</i> CN(92)	<i>ν</i> ₅₄	1034	1038	17	18	<i>ν</i> ₅₇	1091	1088	11	4	<i>ν</i> ₅₇	1106	1103	5	1
	<i>ν</i> ₅₈	980	980	2	4	<i>ν</i> CH ₃ (86), <i>ν</i> NH ₃ (12)	<i>ν</i> ₅₈	867	864	1	4	<i>ν</i> ₅₈	841	845	4	4	<i>ν</i> ₅₈	1027	1027	21	18
	<i>ν</i> ₅₉	901	880	4	4	<i>ν</i> CC(61), <i>ν</i> CN(15)	<i>ν</i> ₅₉	823	830	1	3	<i>ν</i> ₅₉	804	812	0	4	<i>ν</i> ₅₉	768	765	1	1
	<i>ν</i> ₆₀	820	812	4	4	<i>ν</i> CH ₃ (59), <i>ν</i> NH ₃ (37)	<i>ν</i> ₆₀	775	777	1	0	<i>ν</i> ₆₀	600	595	0	0	<i>ν</i> ₆₀	788	790	0	0
	<i>ν</i> ₆₁	751	750	3	3	<i>ν</i> NH ₃ (93)	<i>ν</i> ₆₂	585	587	5	5	<i>ν</i> ₆₁	766	748	4	2	<i>ν</i> ₆₁	639	645	4	4
	<i>ν</i> ₆₂	731	728	2	2	<i>ν</i> NH ₃ (64), <i>ν</i> CH ₃ (35)	<i>ν</i> ₆₃	580	587	5	5	<i>ν</i> ₆₂	715	719	1	0	<i>ν</i> ₆₂	573	570	2	7
	<i>ν</i> ₆₃	663	664	8	8	<i>δ</i> NCC(59), <i>δ</i> RhNC(22)	<i>ν</i> ₆₁	648	650	6	7	<i>ν</i> ₆₃	637	630	8	8	<i>ν</i> ₆₁	551	544	3	3
	<i>ν</i> ₆₄	507	506	13	9	<i>ν</i> RhN(64), <i>δ</i> RhNC(14), <i>δ</i> NCC(13)	<i>ν</i> ₆₄	475	475	10	11	<i>ν</i> ₆₄	507	507	13	7	<i>ν</i> ₆₁	622	628	6	10
	<i>ν</i> ₆₅	435	445	7	4	<i>δ</i> NRhN(36), <i>δ</i> RhNC(18), <i>ν</i> ₆₅	<i>ν</i> ₆₅	422	424	5	5	<i>ν</i> ₆₅	432	425	6	5	<i>ν</i> ₆₅	420	413	6	4
	<i>ν</i> ₆₆	402	397	3	3	<i>τ</i> RhN(11), <i>τ</i> CC(10)	<i>ν</i> ₆₆	397	390	3	0	<i>ν</i> ₆₆	400	392	3	0	<i>ν</i> ₆₆	395	398	3	3
	<i>ν</i> ₆₇	359	357	7	4	<i>δ</i> NRhN(26), <i>τ</i> CC(25)	<i>ν</i> ₆₇	343	333	6	2	<i>ν</i> ₆₇	351	348	6	5	<i>ν</i> ₆₇	337	328	5	2
	<i>ν</i> ₆₈	291	296	7	7	<i>δ</i> NRhN(41), <i>ν</i> RhN(20)	<i>ν</i> ₆₈	274	273	5	5	<i>ν</i> ₆₈	286	285	7	8	<i>ν</i> ₆₈	270	270	5	5
	<i>ν</i> ₆₉	173	184	3	3	<i>ν</i> RhN(86)	<i>ν</i> ₆₈	168	176	3	2	<i>ν</i> ₆₈	170	170	3	3	<i>ν</i> ₆₈	165	170	3	1
	<i>ν</i> ₇₀	120	120	0	0	<i>δ</i> NRhN(87)	<i>ν</i> ₆₉	119	113	0	0	<i>ν</i> ₆₉	119	115	0	0	<i>ν</i> ₆₉	118	120	0	5
						<i>δ</i> NRhN(48), <i>τ</i> RhN(40)	<i>ν</i> ₇₀														

^a The fundamentals of the tris(1,2-ethanediamine)rhodium(III) cation have been arranged according to their species with diminishing frequencies, those of the deuterated compounds to give, as far as possible, matching PED's. The stated PED's are only approximative and small contributions have been neglected. ^b Iteration based upon all eight isotopic species. ^c Solvent data used wherever available. ^d Shift following ¹⁵N substitution of all six nitrogen atoms. ^e The PED is defined as $x_{ik} = 100F_{ik}/L_{ik}^{3/2}$.

force constant $F_L = 0.209$ mdyn/rad (*cf.*²² $[\text{Ni}(\text{NH}_3)_6]^{2+}$: 0.09 mdyn/rad) suggest a strong chelation of the ligand.

Normal modes mainly confined to the ligand. From the results given in Table 3 the following values seem to be typical for 1,2-ethanediamine bonded to Rh^{3+} : δCH_2 , 1470 cm^{-1} , ωCH_2 , 1370 cm^{-1} and 1330 cm^{-1} , tCH_2 , 1230 and 1330 cm^{-1} , and ρCH_2 , 820 and 980 cm^{-1} . The results of free 1,2-ethanediamine based upon *cis* C_{2v} symmetry,^{24,25} later proved incorrect,^{26,27} correspond to the following ranges: δCH_2 , 1445–1469, ωCH_2 , 1298–1318, tCH_2 , 880–1360, and ρCH_2 , 761–815 cm^{-1} . The only major discrepancy concerns the assignment of a tCH_2 mode to 880 cm^{-1} in free 1,2-ethanediamine²⁵ which appears to be too low. Previous assignments of the modes in $[\text{Rh}(\text{en})_3]^{3+}$ complexes have been based upon the results of *N*-deuteration^{28,29} using polarized radiation.³⁰

Our calculations confirm the coupling between the two amine groups of 1,2-ethanediamine to be much smaller, and the separation between the in-phase and the out-of-phase combination usually does not exceed 50 cm^{-1} . The following regions are typical for 1,2-ethanediamine chelated to Rh^{3+} : δNH_2 , 1600–1610 cm^{-1} , tNH_2 , 1290–1310 cm^{-1} , ωNH_2 , 1165–1185 cm^{-1} , and ρNH_2 , 730–780 cm^{-1} . As before, these regions apply only to modes which are reasonably localized; they may easily be displaced by 100 cm^{-1} upon coupling with neighbouring modes. The δNH_2 mode in $[\text{Rh}(\text{en})_3]^{3+}$ chelates has been attributed by other authors to bands in the 1500–1600 cm^{-1} region.^{28,29} This can hardly be correct since (i) the bands in this region (in contrast to the results described recently by Gouteron³⁰) disappear by removal of the coordinated water, (ii) the bands are not observed in solution (*cf.* Krishnan and Plane³¹) and (iii) these assignments disagree with the results of the normal coordinate analysis, which consistently place them above 1600 cm^{-1} .

The C–C and C–N stretching vibrations in $[\text{Rh}(\text{en})_3]^{3+}$ are coupled to other vibrations, but the C–N stretching modes are usually found in the region 1020–1070 cm^{-1} . Previous assignments have been based upon comparison with free 1,2-ethanediamine, and locate the modes in question within the region 1000–1100 cm^{-1} .^{28,29}

Normal modes mainly confined to the central RhN₆ region. The six rhodium-nitrogen stretching coordinates form a basis with the reduced representation: $A_1 + A_2 + 2E$ of the point group D_3 . Previous investigations^{28,30} have identified the symmetrical Rh–N stretching vibration of species A_1 as the very strong Raman band at *ca.* 545 cm^{-1} . Our calculations confirm this band to consist mainly of $\nu_2\text{RhN}$ (68 %), but weakly coupled to the δNCC (11 %) and δRhNC (14 %) deformational modes. Inspection of the L matrix shows that stretching of the RhN bonds is followed by a closing of the RhNC angles and opening of the NCC angles in such a way that the distance between the rhodium atom and the midpoint of the C–C bond is almost unaltered. It should be noted that this band is unambiguously identified by the major shift on ¹⁵N substitution (Table 3). It has recently been proposed³² that the other strong fundamental of species A_1 in the 280–320 cm^{-1} region of the Raman spectra of tris(ethylenediamine) complexes (*i.e.* ν_{17} at 272 cm^{-1}) should have substantial RhN stretching character. This is not confirmed by our calculations, which indicate the contribution of $\nu_5\text{RhN}$ to this band to be only 12 %.

Our calculations show that two bands near 450 cm^{-1} in $[\text{Rh}(\text{en})_3]^{3+}$ attributed³⁰ to species A_2 and E can be assigned as the fundamentals ν_{33} and ν_{35} . The former of these arises from $\nu_{25}\text{RhN}$ (84 %) coupled to δNCC (14 %), *i.e.* corresponds to an almost pure Rh–N stretching vibration of species A_2 . This was previously assigned^{28–30} to bands at *ca.* 100 cm^{-1} higher frequencies.

One of the Rh–N stretching vibrations of species E was attributed²⁹ to a band near 500 cm^{-1} , but this band was assigned by Gouteron³⁰ to a ligand deformation. The major shifts observed on ¹⁵N substitution (Table 3) leave no doubt that this band must arise mainly from Rh–N stretching. However, the calculations indicate that in addition to νRhN (64 %) the PED contains δNCC (13 %) and δRhNC (14 %), and accordingly the fundamental comprises both proposals mentioned above. The other Rh–N stretching vibration of species E is calculated to lie around 290 cm^{-1} , which complies with a weak band in the spectrum of $[\text{Rh}(\text{en})_3]^{3+}$ but may very well need future revision since the ¹⁵N shifts are not decisive.

The remaining fundamentals of this region show no features of special interest. However, it should be mentioned that the fundamental ν_{32} of species A_2 was previously attributed to Rh-N stretching²⁸⁻³⁰ while our calculations indicate mainly ring deformation coupled to CH_2 rocking. On successive removal of 1, 2, and 3 hydrogen atoms with KNH_2 this band is displaced towards higher frequencies.²³ Since coordination of ethylenediamine anions is undoubtedly much stronger than coordination of neutral ethylenediamine, this shift merely reflects the increase in force constants for δRhNC and δNCC following deprotonation.

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