

Metal Complexes with Mixed Ligands. 9. The Crystal Structure of Aquatrisimidazolecopper(II) Sulphate, $\text{Cu}(\text{H}_2\text{O})(\text{C}_3\text{H}_4\text{N}_2)_3\text{SO}_4$

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The crystal structure of $\text{Cu}(\text{H}_2\text{O})(\text{C}_3\text{H}_4\text{N}_2)_3\text{SO}_4$ has been determined from three-dimensional X-ray diffraction data. The crystals are monoclinic, spacegroup $P2_1/n$, with unit cell dimensions and corresponding standard deviations (at 25 °C) $a = 14.239(1)$ Å; $b = 8.707(1)$ Å; $c = 11.717(1)$ Å and $\beta = 90.244(5)^\circ$. There are four formula units per unit cell. Intensities were collected and measured with the linear diffractometer PAILRED using $\text{MoK}\alpha$ radiation. The structure was solved by routine heavy-atom methods and refined by full matrix least-squares methods. With positional coordinates of all atoms and anisotropic thermal factors of non-hydrogen atoms as parameters the structure was refined to a conventional R -value of 0.043. The refinement was based on 3032 observations. The distorted octahedron around copper is formed by four short bonds from three imidazole nitrogens and one sulphate oxygen and two longer bonds formed by one sulphate oxygen and the water oxygen. The sulphate group forms a bridge between copper atoms leading to infinite chains along the two-fold screw axes. Both within and between the chains there are hydrogen bonds between the nitrogens not coordinated to copper atoms, the sulphate oxygens, and the water oxygen.

The investigation of metal-imidazole-complexes forms the basis of a research programme at this department which aims at determining the different possible coordinations of the histidine residue imidazole to metal atoms as models for the more complex biological systems where metal atoms interact with histidine residues. The formation of Cu(II)-imidazole complexes with different anions have been studied especially, both in the crystalline state and in solution.¹⁻⁸

When the ratio of imidazole to copper is varied, mononuclear complexes are formed in

solution where the number of imidazole rings bound to Cu(II) varies from one to six. If the anion medium is varied, most of the complexes with a composition corresponding to these mononuclear species can crystallize. At this stage the crystal structures of Cu(II)-imidazole complexes with Cl^- , ClO_4^- and SO_4^{2-} have been determined.²⁻⁴ They contain complexes with the ratio $\text{C}_3\text{H}_4\text{N}_2:\text{Cu} = 2:1$, $3:1$, and $4:1$. Two complexes have been crystallized with PO_4^{3-} as anion and the chemical analyses correspond to the formulas $\text{Cu}(\text{C}_3\text{H}_4\text{N}_2)_5\text{HPO}_4 \cdot 5\text{H}_2\text{O}$ and $\text{Cu}(\text{C}_3\text{H}_4\text{N}_2)_6(\text{H}_2\text{PO}_4)_2 \cdot 2\text{H}_2\text{O}$. The structure determinations of these are in progress and may possibly confirm the suggested 5:1 and 6:1 coordinations. In the sulphate medium two different species have so far been crystallized; the first was $\text{Cu}(\text{C}_3\text{H}_4\text{N}_2)_3\text{SO}_4$ ⁵ and the other is $\text{Cu}(\text{H}_2\text{O})(\text{C}_3\text{H}_4\text{N}_2)_3\text{SO}_4$ which is the subject of this communication.

EXPERIMENTAL

Crystal preparation and analysis. In a typical preparation of the crystals 30 ml of a 1 M imidazole solution were added to 10 ml of 1 M CuSO_4 solution and the pH of the mixture was adjusted to about 6.5 by adding 0.1 M sulphuric acid. The solution was left to evaporate at room temperature and after a few days blue crystals, in the shape of well-defined prisms, were formed. They were not stable in air. The copper content was determined by titration with EDTA,⁹ and the nitrogen content was determined using the Kjeldahl method.¹⁰ With the aid of IR-spectra the presence of H_2O was indicated. Using a thermal balance it could be shown that the crystals lose one water molecule per formula unit after heating to 130–140 °C. The following analyses (in weight-%) were obtained. Found: Cu 16.4; N 21.7; H_2O 4.6. Calc. for $\text{Cu}(\text{H}_2\text{O})$ -

(C₃H₄N₂)₃SO₄: Cu 16.6; N 22.0; H₂O 4.7. The density of the crystals was determined by flotation (using bromoform and xylene) to be 1.73 g/cm³. With four units of Cu(H₂O)(C₃H₄N₂)₃SO₄ in the unit cell the calculated density is 1.74 g/cm³.

Unit cell data and spacegroup. From rotation photographs around the *a*- and *b*-axes and corresponding Weissenberg photographs (*0kl*–*2kl* and *h0l*–*h2l*) taken with CuK α -radiation, it was concluded that the crystals are monoclinic. The systematic extinctions for *h0l* when *h*+*l* is odd and for *0k0* when *k* is odd are characteristic for the spacegroup *P2₁/n* (No. 14).¹¹ The dimensions of the unit cell were determined with the aid of powder photographs taken with a camera of Guinier-Hägg type using 45 observations in a least-squares refinement. The following parameters and corresponding standard deviations were obtained: *a* = 14.239(1) Å; *b* = 8.707(1) Å; *c* = 11.717(1) Å; and β = 90.244(5)°.

Collection and reduction of intensity data. The intensities were measured with an automatic linear diffractometer (PAILRED) using MoK α -radiation, graphite monochromator and pulse height discriminator. The specimen crystal was enclosed, together with part of the crystallization mother liquid, in a sealed capillary of Lindeman glass. It was mounted around the *b*-axis and about 4300 independent reflexions from ten reciprocal levels (*h0l*–*h9l*) were measured. All reflexions with counts less than 10 000 were measured up to three times; background radiation was measured for 40 s on each side of every reflexion. For the *h0l* layer the half-scan ranges were 1.1° and 1.4° for $\theta \geq 22^\circ$ (ω_1) and $\theta < 22^\circ$ (ω_2) respectively. The half-scan ranges were then gradually increased to the value of 1.3° and 1.8° for the *h9l*-layer. The scan speed used was 1 deg./min.

The intensities were corrected according to the relation $I = TI/N - \omega(B_1 + B_2)/t_B v$ where *I* = net intensity, *TI* = total intensity (peak + background), *N* = number of scans over the reflexion, ω = the half-scan range, *B*₁ and *B*₂ = background intensities, *t_B* = time for background measure-

ment and *v* = scan speed. The relative counting statistical error of each reflexion $\Delta I/I$ was calculated using the formula

$$\frac{\Delta I}{I} = \frac{[TI/N^2 + (\omega/t_B v)^2(B_1 + B_2) + (T^2/N^2) \times 0.0001]^{1/2}}{TI/N - [\omega(B_1 + B_2)]/t_B v}$$

where $(T^2/N^2) \times 0.0001$ is a term that corrects for the linear error in the diffractometer. Of 4300 measured reflexions 3032 were significant at the 95 % level, *i.e.* had $\Delta I/I < 0.50$. Lp and absorption corrections were then applied. The linear absorption coefficient is 17.29 cm⁻¹ for MoK α -radiation; there was thus a variation in the transmission factors of 11 %.

The calculations were performed with a CDC 3300 computer using modified versions of the programmes mentioned by Ivarsson, Lundberg and Ingri.⁴

STRUCTURE DETERMINATION AND REFINEMENT

The position of the copper atom was found from the three-dimensional Patterson synthesis. Heavy atom Fourier methods allowed the determination of the approximate positions of the other non-hydrogen atoms. However, to distinguish N(2), N(4), and N(6) from C(2), C(5), and C(8) (see Fig. 1 for numbering) all six atoms were refined as carbons and then the group of three atoms with the lower temperature factors was labelled nitrogen prior to further refinement.

The atomic coordinates and anisotropic temperature factors were refined using full matrix least-squares techniques. The reflexions were weighted according to the method suggested by Cruickshank,¹² $\omega = 1/(a + |F_o| + c|F_o|^2 + d|F_o|^3)$ using constants $a = 100$, $c = -0.02$, $d = 0.0006$.

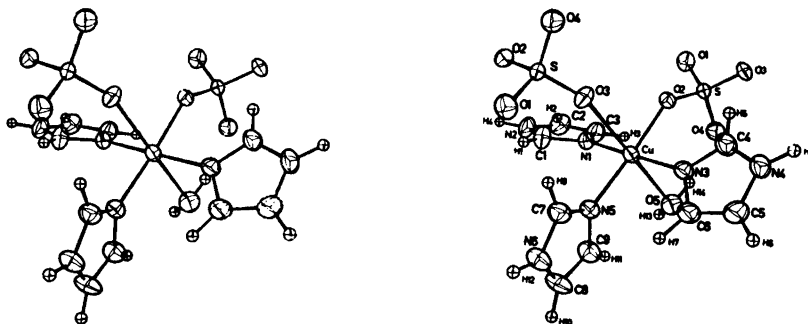


Fig. 1. A stereoscopic illustration of a molecule viewed along the *a*-axis. Thermal ellipsoids are scaled to enclose 50 % probability. The parenthesis around the numbers are omitted in the figure.

Table 1a. Fractional atomic coordinates and anisotropic thermal parameters. Their estimated standard deviations are given in parentheses. All values are multiplied by 10^4 . Anisotropic temperature factors have been calculated according to the formula $\exp[-(h^2\beta_{11} + k^2\beta_{22} + l^2\beta_{33} + hk\beta_{12} + hl\beta_{13} + kl\beta_{23})]$.

	<i>x</i>	<i>y</i>	<i>z</i>	β_{11}	β_{22}	β_{33}	β_{12}	β_{13}	β_{23}
Cu	2792(0.3)	1506(0.5)	746(0.3)	29(0.2)	59(1)	38(0.3)	-15(0.5)	-14(0.3)	22(1)
S	1079(1)	4198(1)	2495(1)	25(0.3)	49(1)	33(0.5)	2(1)	0(1)	-6(1)
O1	4572(2)	-148(3)	3356(2)	32(1)	83(4)	63(2)	3(3)	-32(3)	-11(4)
O2	3259(2)	423(3)	2158(2)	34(1)	68(3)	41(1)	12(3)	-10(2)	19(4)
O3	1586(2)	2901(3)	2011(2)	40(1)	65(3)	46(2)	19(3)	6(2)	-30(4)
O4	539(2)	3678(3)	3509(2)	46(1)	84(4)	51(2)	-2(4)	39(3)	-4(4)
O5	3896(2)	113(4)	-513(2)	40(1)	117(5)	63(2)	4(4)	6(3)	-8(5)
N1	3734(2)	3159(3)	1056(2)	33(1)	52(4)	46(3)	-9(3)	2(3)	3(4)
N2	4344(3)	5417(4)	1367(3)	55(2)	62(5)	70(3)	-26(5)	13(4)	-33(5)
C1	3564(3)	4640(5)	1096(4)	38(2)	74(5)	72(3)	4(5)	9(4)	-5(6)
C2	5047(3)	4384(5)	1513(4)	37(2)	110(6)	67(3)	-28(5)	-3(4)	-20(7)
C3	4664(2)	2993(5)	1321(3)	33(2)	78(5)	59(3)	-3(4)	-6(3)	-16(6)
N3	1884(2)	-201(3)	441(2)	30(1)	74(4)	34(2)	-13(3)	-1(2)	12(4)
N4	1113(2)	-2372(4)	618(3)	42(2)	82(5)	60(2)	-39(4)	-5(3)	23(5)
C4	1748(3)	-1428(5)	1082(3)	38(2)	87(5)	51(2)	-35(5)	-7(3)	17(6)
C5	811(3)	-1711(5)	-379(3)	47(2)	119(7)	54(3)	-43(6)	-24(4)	-4(6)
C6	1290(3)	-392(5)	-484(3)	46(2)	100(6)	45(2)	-47(5)	-27(4)	16(6)
N5	2315(2)	2685(4)	-597(7)	29(1)	81(4)	40(2)	-7(4)	-2(2)	23(4)
N6	1374(2)	3980(4)	-1710(3)	41(2)	121(5)	50(2)	15(5)	-15(3)	39(5)
C7	1522(2)	3464(5)	-647(3)	34(2)	94(5)	44(2)	-14(5)	-11(3)	15(6)
C8	2101(3)	3506(6)	-2373(3)	53(2)	164(8)	44(3)	11(7)	4(4)	65(7)
C9	2689(3)	2707(5)	-1679(3)	36(2)	122(6)	53(3)	21(5)	15(3)	31(6)

Table 1b. Fractional atomic coordinates and isotropic thermal parameters for the hydrogen atoms. Their estimated standard deviations are given in parentheses. All coordinates are multiplied by 10^4 .

	<i>x</i>	<i>y</i>	<i>z</i>	$B(\text{\AA}^2)$
H1	2991(33)	5132(62)	951(43)	4.3(1.1)
H2	5655(40)	4678(75)	1655(51)	6.1(1.4)
H3	4935(31)	2016(58)	1287(39)	3.6(1.0)
H4	4413(35)	6335(62)	1446(44)	4.5(1.1)
H5	1998(35)	-1500(61)	1775(43)	4.6(1.2)
H6	336(35)	-2096(66)	-877(44)	4.9(1.2)
H7	1237(29)	379(53)	-1067(37)	3.2(0.9)
H8	906(33)	-3221(59)	980(41)	4.1(1.1)
H9	1151(33)	3743(57)	-2(40)	3.8(1.0)
H10	2142(38)	3762(67)	-3161(46)	5.3(1.3)
H11	3236(30)	2330(54)	-1840(37)	3.3(0.9)
H12	842(31)	4503(58)	-1914(39)	3.8(1.0)
H13	4451(38)	571(74)	-837(48)	5.8(1.4)
H14	4179(41)	-405(79)	23(53)	6.5(1.5)

The atomic scattering factors for Cu^{2+} , S, O, N, and C were taken from the International Tables.¹⁴ Account was taken of the real part of the dispersion correction for Cu^{2+} and S. Refinement, not including hydrogen atoms, was terminated at an R -value = $(\sum |F_o| - |F_c|) / \sum |F_o| = 0.049$.

A difference Fourier map was then calculated and peaks on it could be postulated as being due to hydrogen atoms. Refinement including the hydrogen coordinates and their isotropic thermal parameters was made, using the scattering factors proposed by Stewart, Davidson and Simpson.¹⁵ This was terminated when all param-

Table 2. Observed and calculated structure factors ($\times 10$).

L H	L H	L H	L H	L H	L H	L H	L H
K= 0							
6-16	192 188	0 6	333 358	10 6	143 137	6 12	167 160
6-14	157 161	0 4	528 554	10 5	141 133	3 1	1077 1005
6-12	330 330			10 4	311 315	6 9	641 641
6-10	470 470	K= 1		10 3	214 203	6 8	399 408
6-8	98 102			10 2	171 179	6 7	569 569
6-6	104 105	17 -2	82 80	10 1	404 405	6 6	314 320
6-4	548 528	17 2	77 114	10 0	119 132	6 5	105 100
6-2	1285 1269	16 4	117 121	10 -2	402 416	6 4	242 229
6 0	1602 991	16 2	110 110	10 -4	240 239	6 3	184 168
6 2	874 824	16 0	138 137	10 -5	348 357	6 1	228 208
6 4	289 300	16 0	155 164	10 -6	98 96	6 0	104 111
6 6	633 641	16 -2	208 213	10 -7	143 145	6 -1	511 498
6 8	564 549	16 -4	95 113	10 -9	107 104	6 -2	428 426
6 10	399 384	16 -5	79 93	10 -11	98 95	6 -3	566 545
6 12	274 265	16 -8	83 94	10 -12	115 98	6 -4	122 221
6 14	217 215	15 -9	117 110	10 -14	146 147	6 -5	122 120
6 16	242 221	15 -6	183 189	10 -15	187 186	6 -6	285 303
5 19	136 117	15 -4	172 174	9 -11	171 180	6 -7	124 116
5 17	98 89	15 -3	128 134	9 -10	70 75	6 -8	84 96
5 16	143 138	15 -1	132 143	9 -9	298 308	6 -9	473 483
5 13	194 180	15 0	80 88	9 -8	119 115	6 -10	210 218
5 11	834 824	15 1	83 89	9 -7	339 361	6 -12	285 289
5 9	582 581	15 4	96 76	9 -6	534 539	6 -14	74 63
5 7	177 170	15 6	135 121	9 -5	154 144	6 -16	81 71
5 5	102 103	15 9	131 131	9 -4	284 287	6 -18	105 100
5 3	450 419	14 11	90 88	9 -3	571 570	6 -19	105 100
5 -1	1014 993	14 10	136 140	9 -1	409 401	5 -18	70 61
5 -3	317 307	5 -3	1030 1009	9 0	183 183	5 -17	95 91
5 -5	127 82	14 7	152 160	9 2	267 256	5 -16	135 152
5 -14	102 109	14 5	129 139	9 1	150 160	5 -15	142 146
5 -12	284 278	14 5	207 218	0 4	336 352	5 -14	143 146
5 -10	159 149	5 -13	203 196	14 4	106 115	5 -13	395 401
5 -8	102 93	5 -17	205 217	14 3	111 118	5 -12	158 148
5 -6	67 67	5 -19	160 150	14 2	100 108	5 -11	505 522
5 -4	85 87	14 1	121 121	14 1	32 32	5 -10	561 560
5 -2	289 286	14 -1	82 88	14 -1	71 81	5 -9	158 160
5 2	273 276	14 -4	569 565	14 -3	138 128	5 -8	299 298
5 4	368 376	4 -12	650 650	14 -5	206 209	5 -7	343 341
5 6	580 570	4 -10	151 162	14 -7	82 64	5 -6	408 387
5 8	282 272	4 -8	112 129	14 -8	111 129	5 -5	267 272
5 10	164 166	4 -6	175 170	14 -10	155 152	5 -4	182 181
5 11	370 370	4 -4	583 541	14 -11	81 83	5 -2	197 177
5 9	359 369	4 2	612 566	13 -12	155 145	5 -1	217 231
5 7	88 77	4 2	119 103	13 -11	76 64	5 0	188 186
5 5	240 249	4 4	1258 1260	13 -9	160 175	5 1	233 233
5 3	195 201	4 6	611 628	13 -5	113 125	5 2	157 193
5 1	237 227	4 8	381 381	13 -3	199 206	5 3	710 687
5 -1	114 99	4 10	1058 1042	13 -2	204 207	5 4	481 477
5 -3	180 188	4 12	477 466	13 -1	171 174	5 5	974 981
5 -5	448 463	4 14	77 44	13 1	286 307	5 7	786 791
5 -7	384 391	4 20	312 106	13 3	245 247	5 8	422 441
5 -9	85 80	3 19	159 156	13 4	258 267	5 9	270 281
5 -11	152 150	3 17	135 126	13 5	145 139	5 10	187 176
5 -14	189 188	3 15	232 229	13 6	141 142	5 11	178 183
5 -16	354 358	3 13	506 510	13 7	118 128	5 12	82 72
5 -18	477 495	3 9	75 52	13 13	107 83	5 13	78 48
5 -20	305 314	3 7	378 381	12 14	135 125	5 15	75 73
5 -22	107 122	3 5	676 664	12 12	218 214	5 19	107 78
5 0	553 553	3 3	1301 1292	12 11	142 133	5 20	127 106
5 2	187 201	3 1	85 74	12 10	168 172	4 20	101 71
5 4	468 474	3 -1	1388 1390	12 9	191 194	4 19	82 101
5 6	187 193	3 -3	839 831	12 8	162 168	4 17	79 75
5 8	462 457	3 -5	809 806	12 7	154 150	4 16	222 221
5 10	379 359	3 -7	114 125	12 6	211 215	4 14	325 322
5 12	74 52	3 -9	125 128	12 5	81 76	4 13	222 218
5 14	213 211	3 -11	207 198	12 4	75 70	4 12	223 230
5 16	317 318	3 -13	462 474	12 3	160 167	4 10	469 425
5 18	312 312	3 -15	324 318	12 2	68 67	4 9	92 79
5 20	336 339	3 -17	79 56	12 1	389 400	4 8	205 205
5 3	532 530	2 -20	138 129	12 -3	260 268	4 7	419 415
5 5	108 180	2 -16	141 133	12 -4	335 338	4 6	443 437
5 7	486 506	2 -14	225 221	12 -6	196 186	4 5	221 203
5 9	714 720	2 -12	402 399	12 -7	90 88	4 4	193 208
5 11	141 141	2 -10	457 445	12 -8	79 78	4 3	1103 1081
5 13	314 305	2 -8	456 464	12 -9	172 172	4 2	814 769
5 15	189 189	2 -6	825 823	12 -12	156 151	4 1	458 431
5 17	232 230	2 -4	458 455	12 -13	103 112	4 0	311 326
5 19	288 282	2 -2	1533 1488	11 -13	245 233	4 -1	311 326
5 16	97 91	2 0	203 199	11 -11	126 125	4 -2	881 871
5 14	169 163	2 2	272 258	11 -10	184 196	4 -3	356 358
5 12	348 353	2 4	131 128	11 -9	121 118	4 -4	921 897
5 10	291 296	2 6	248 259	11 -8	185 185	4 -5	786 792
5 8	281 288	2 10	603 582	11 -7	76 76	4 -6	468 458
5 6	803 786	2 12	677 676	11 -5	214 218	4 -7	60 36
5 4	859 864	2 14	403 395	11 -4	216 219	4 -8	211 211
5 2	542 525	2 20	108 100	11 -3	158 161	4 -9	279 275
5 0	607 609	1 19	198 170	11 -2	188 189	4 -10	203 205
5 6	288 288	1 17	245 235	11 -1	150 159	4 -11	156 154
5 8	221 217	1 15	176 170	11 0	78 90	4 -12	292 302
5 10	181 168	1 13	263 251	11 1	166 159	4 -14	182 175
5 12	145 145	1 11	258 262	11 2	263 257	4 -15	201 198
5 14	323 321	1 9	540 547	11 3	181 183	4 -17	195 187
5 16	350 351	1 7	142 142	11 4	179 175	4 -19	157 157
5 18	134 114	1 5	597 588	11 5	327 324	4 -20	128 116
5 20	73 46	1 3	1222 1244	11 6	178 189	3 -19	93 90
5 15	104 102	1 -3	588 563	11 7	307 297	3 -16	141 136
5 13	141 128	1 -5	464 410	11 8	224 230	3 -15	207 214
5 11	76 83	1 -7	142 142	11 9	195 197	3 -14	157 172
5 9	508 502	1 -9	655 654	11 10	214 210	3 -13	92 73
5 7	1028 1006	1 -11	603 598	11 11	165 168	3 -12	286 292
5 5	188 207	1 -13	152 148	11 13	106 126	3 -11	348 356
5 3	344 333	1 -15	337 82	10 16	140 156	3 -10	259 251
5 1	118 205	1 -17	246 243	10 15	192 191	3 -9	478 506
5 -3	719 736	0 20	115 89	10 14	109 116	3 -8	438 431
5 -5	570 553	0 18	337 328	10 13	241 245	3 -7	163 180
5 -7	171 163	0 16	232 225	10 12	113 97	3 -6	756 760
5 -9	250 249	0 14	76 55	10 10	171 171	3 -5	665 638
5 -11	15 177	0 12	397 410	10 9	191 182	3 -4	157 172
5 -13	79 43	0 10	121 131	10 8	117 112	3 -3	1199 1194
5 -15	231 217	0 8	284 279	10 7	177 184	3 -2	396 382

Table 2. Continued.

L	M	L	M	L	M	L	M	L	M	L	M	L	M	
8 -7	391	395	4-15	92	76	1 5	229	252	11 -6	234	237	6 -8	121	126
8 -6	159	162	4-11	528	537	1 +	1242	1275	11 -7	84	90	6 -7	807	812
8 -5	425	447	4-12	223	225	1 3	82	50	11 -8	192	200	6 -6	630	627
8 -3	313	327	4-11	528	537	1 2	1642	1706	11-10	207	206	6 -5	649	635
8 -1	756	736	4-11	223	230	1 -2	146	125	11-12	127	139	6 -4	291	288
8 0	332	319	4-9	675	673	1 -3	49	57	11-13	152	154	6 -3	366	365
8 1	276	277	4 -8	89	110	1 -4	71	149	10-13	70	59	6 -2	158	97
8 2	366	362	4 -7	134	139	1 -5	74	731	10-12	149	148	6 -1	335	315
8 3	237	250	4 -6	155	159	1 -6	447	+66	10-11	101	83	6 2	109	100
8 4	7	58	4 -5	389	462	1 -7	92	70	10 -3	138	156	6 3	154	143
8 5	234	225	4 -4	791	749	1 -8	528	841	10 -2	399	405	6 4	174	157
8 6	237	250	4 -3	64	74	1 -9	10	96	10 -1	390	405	6 5	440	453
8 7	2	58	4 -2	230	230	1-10	220	230	10 0	200	203	6 6	311	315
8 8	234	225	4 -1	224	237	1-11	193	199	10 1	490	502	6 7	201	194
8 9	222	220	4 0	333	231	1-12	315	313	10 2	170	190	6 8	77	79
8 10	414	411	4 1	143	149	1 -13	144	524	10 3	347	347	6 9	188	179
8 11	87	83	4 2	759	720	1-15	90	96	10 4	304	310	6 10	610	619
8 12	203	202	4 3	194	193	1-16	124	124	10 5	332	339	6 12	369	372
8 15	81	101	4 4	506	474	1-18	83	56	10 6	272	277	6 13	328	332
8 17	241	222	4 5	805	792	1-19	79	53	10 11	95	105	6 15	190	184
7 16	72	41	4 6	382	311	0 2	2	844	10 12	48	52	6 16	87	91
7 15	130	124	4 7	1004	1031	0 3	1477	1510	10 13	141	136	6 18	101	84
7 12	292	284	4 8	389	401	0 4	670	707	10 15	203	193	6 18	157	153
7 11	115	198	4 9	314	331	0 5	754	778	9 15	119	119	5 17	158	153
7 10	389	394	4 10	160	160	0 6	261	253	9 14	105	103	5 16	86	89
7 9	136	140	4 11	67	92	0 8	203	185	9 12	264	261	5 15	148	160
7 8	129	143	4 12	149	149	0 9	129	213	9 11	93	99	5 11	75	61
7 7	68	74	4 13	341	349	0 10	142	153	9 10	338	344	5 10	190	195
7 6	456	449	4 14	115	107	0 13	215	212	9 9	9	124	5 9	386	393
7 5	390	391	4 15	107	107	0 14	191	192	9 8	331	334	5 8	245	253
7 4	987	949	3 19	120	114	0 15	298	302	9 6	183	172	5 7	369	363
7 3	196	187	3 8	950	892	15 -3	131	124	9 5	16	171	5 6	363	375
7 2	555	536	3 7	105	111	0 17	93	91	9 4	304	290	5 5	510	500
7 1	196	192	3 16	266	258	0 19	149	138	9 1	363	295	5 4	425	443
7 0	377	355	3 14	181	170	0 20	107	98	9 0	189	190	5 3	101	93
7 -1	190	172	3 13	89	105	16 -2	121	128	9 -3	304	242	5 2	944	910
7 -2	375	356	3 12	124	120	16 -1	111	120	9 -2	152	146	5 1	152	144
7 -3	482	462	3 10	107	104	16 0	111	120	9 -1	494	502	5 0	199	197
7 -4	78	50	3 10	107	104	16 -2	121	128	9 -5	212	213	5 -1	359	334
7 -5	224	210	3 9	153	156	16 -1	111	120	9 -6	343	353	5 -2	534	498
7 -6	555	563	3 8	444	452	16 0	3	172	9 -7	96	104	5 -3	378	364
7 -7	367	369	3 7	255	268	15 5	84	85	9 -8	168	176	5 -4	359	369
7 -8	530	527	3 6	197	180	15 4	93	100	9 -9	198	197	5 -5	445	448
7 -9	128	129	3 5	164	172	15 1	74	78	9-10	261	266	5 -6	361	353
7 -10	213	218	3 4	67	70	15 0	107	87	9 -13	91	94	5 -7	220	217
7 -11	64	61	3 3	2	663	633	15 -1	120	9 -15	89	69	5 -8	371	362
7 -12	215	213	3 2	324	312	15 -2	157	176	9 -16	116	105	5 -9	432	435
7 -13	96	91	3 0	950	892	15 -3	131	124	8 -15	193	192	5 -10	292	294
7 -14	224	223	3 -1	625	608	15 -4	129	125	8 -13	142	135	5 -11	97	103
7 -15	90	88	3 -2	559	539	15 -5	162	156	8 -11	240	234	5 -13	133	137
7 -16	95	81	3 -3	709	685	15 -8	86	93	8 -10	135	131	5 -14	186	185
7 -18	73	71	3 -4	468	445	14 -10	102	92	8 -9	301	301	5 -15	137	142
6 -17	90	80	3 -5	332	322	14 -9	123	116	8 -8	337	345	5 -17	205	206
6 -15	211	221	3 -6	383	398	14 -8	149	151	8 -7	79	78	5 -18	109	97
6 -14	146	133	3 -7	551	563	14 -7	191	192	8 -6	231	236	5 -19	72	42
6 -13	262	266	3 -8	75	72	14 -2	177	140	8 -5	309	293	4 -19	182	172
6 -12	110	106	3 -9	166	178	14 -1	178	170	8 -4	124	130	4 -18	103	99
6 -11	81	58	3 -10	338	358	14 2	78	119	8 0	79	92	4 -17	193	178
6 -10	83	76	3 -11	146	146	14 3	146	145	8 -1	277	274	4 -15	227	224
6 -9	73	53	3 -12	239	247	14 4	184	178	8 2	371	360	4 -14	84	99
6 -8	290	296	3 -13	65	57	14 5	98	75	8 3	778	758	4 -12	316	320
6 -7	178	190	3 -14	133	128	14 7	104	107	8 4	76	72	4 -10	176	174
6 -6	112	94	3 -15	183	192	14 9	135	129	8 5	500	499	4 -9	123	128
6 -5	274	268	3 -16	268	264	14 10	93	89	8 6	74	67	4 -8	8	8
6 -4	357	361	3 -17	132	127	13 9	74	48	8 7	233	236	4 -7	441	453
6 -3	538	533	3 -18	203	191	13 8	113	98	8 8	150	158	4 -6	179	171
6 -2	59	59	3 -19	97	82	13 6	131	125	8 9	87	85	4 -5	148	115
6 -1	312	305	2 -19	160	124	13 5	105	91	4 -3	570	560	4 -4	570	560
6 0	268	267	2 -18	184	184	13 4	130	124	4 -2	110	110	4 -3	110	110
6 1	529	514	2 -17	108	185	13 3	116	125	8 12	88	91	4 -1	1026	994
6 2	713	699	2 -15	107	102	13 2	229	227	8 13	91	89	4 0	504	465
6 3	329	331	2 -14	64	70	13 1	194	149	8 15	125	99	4 1	849	805
6 4	755	742	2 -11	231	234	13 0	283	291	8 16	87	81	4 2	193	168
6 5	185	190	2 -10	179	193	13 -2	77	90	8 17	204	199	4 3	656	630
6 6	208	220	2 -9	307	310	13 -4	119	133	7 14	212	197	4 4	115	108
6 7	136	142	2 -8	233	228	13 -12	113	92	7 13	125	113	4 5	444	492
6 8	86	89	2 -7	1058	1054	12 -12	103	86	7 12	313	321	4 6	7	63
6 9	143	135	2 -6	753	728	12 -10	80	84	7 11	167	157	4 7	175	180
6 10	301	300	2 -5	1011	1018	12 -9	163	140	7 10	282	290	4 8	143	142
6 11	110	116	2 -4	97	85	12 -8	230	239	7 9	96	106	4 9	291	296
6 12	200	204	2 -3	711	695	12 -6	162	160	7 8	176	179	4 14	146	140
6 15	86	79	2 -2	223	216	12 -5	224	230	7 7	68	65	4 15	238	234
6 16	219	212	2 -1	317	312	12 -3	144	135	7 6	266	275	4 16	171	176
6 17	67	70	2 0	487	435	12 -2	130	139	7 5	544	545	4 17	234	232
6 18	442	444	2 1	1196	1149	12 -1	277	286	7 3	118	113	4 19	124	116
5 13	228	224	2 3	213	212	12 0	160	151	7 2	669	671	3 19	81	82
5 12	262	267	2 4	307	298	12 1	201	202	7 1	475	464	3 16	116	119
5 10	79	84	2 5	378	387	12 2	352	360	7 0	73	71	3 15	101	91
5 9	96	88	2 6	5	171	171	12 6	171	7 -2	281	297	3 14	181	185
5 8	587	601	2 7	352	346	12 7	85	91	7 -3	191	190	3 13	80	100
5 7	131	123	2 8	66	56	12 9	168	166	7 -4	199	400	3 12	160	162
5 6	523	513	2 9	359	384	12 11	142	150	7 -5	478	376	3 10	356	360
5 5	457	446	2 10	342	353	12 12	107	98	7 -6	232	235	3 9	346	352
5 4	395	363	2 11	467	469	12 13	246	233	7 -8	88	98	3 8	582	621
5 3	559	564	2 12	257	293	11 13	76	65	7 -9	277	279	3 7	115	120
5 0	740	713	2 15	226	221	11 11	76	96	7 -10	65	95	3 6	754	775
5 -2	300	319	2 16	128	122	11 10	129	12						

Table 2. Continued.

L	H	L	H	L	H	L	H	L	H	L	H	L	H	L	H	L	H	L	H							
K= 4		4-13	89	91	1-5	167	187	10	3	110	114	6	10	443	457	2-6	84	98	10	8	349	363				
		4-10	135	113	1-1	158	135	10	4	157	184	6	11	252	259	2-5	387	377	10	11	277	135				
		4-9	95	107	1-7	186	198	10	5	94	104	6	12	194	182	2-3	502	469	10	11	81	93				
		4-8	558	569	1-9	461	465	10	6	91	100	6	13	154	156	2-2	730	713	10	12	90	84				
		4-7	526	520	1-10	434	431	10	8	123	132	6	14	146	157	2-1	292	293	9	11	107	108				
		4-6	309	309	1-11	420	422	10	10	91	74	6	15	93	98	2	0	434	413	9	8	85	71			
		4-5	177	182	1-12	306	317	10	12	126	130	6	16	177	166	2	1	137	125	9	7	372	366			
		4-4	308	289	1-13	93	75	10	13	79	66	6	17	146	142	2	2	494	500	9	6	164	163			
		4-3	437	420	1-14	199	187	10	14	94	56	6	18	163	157	2	3	451	476	9	5	153	157			
		4	0	93	96	1-16	105	112	10	15	86	78	6	19	89	86	2	4	772	806	9	4	151	143		
		4	1	53	15	1-17	124	136	9	15	73	59	6	20	78	36	2	5	245	255	9	3	143	155		
		4	2	462	476	1-18	77	83	9	13	211	215	6	21	180	177	2	6	1077	1173	9	2	87	80		
		4	3	605	597	0	2	426	459	9	12	40	47	6	22	132	139	2	7	162	149	9	1	374	371	
		4	4	444	434	0	3	290	251	9	11	233	225	6	23	96	89	2	8	333	362	9	0	194	197	
		4	5	177	200	0	4	303	329	9	10	97	76	6	24	368	389	2	9	108	107	9	-1	408	402	
		4	6	88	96	0	5	114	125	9	9	136	147	6	25	221	233	2	10	70	76	9	-2	163	166	
		4	7	119	128	0	6	198	216	9	7	270	270	6	26	195	192	2	12	90	95	9	-4	110	106	
		4	8	370	391	0	7	449	474	9	5	374	515	6	27	182	182	2	16	147	147	9	-5	83	72	
		4	9	194	200	0	10	139	144	9	4	180	195	6	28	363	357	2	18	81	69	9	-7	150	154	
		4	10	210	213	0	11	306	315	9	2	254	254	6	29	474	465	1	17	113	112	9	-8	93	84	
		4	11	372	389	0	12	150	155	9	1	237	240	6	30	340	333	1	16	97	110	9	-9	157	158	
		4	13	95	95	0	13	131	132	9	0	81	88	6	31	701	674	1	15	256	261	9	-11	195	200	
		4	15	71	81	0	14	265	263	9	-1	243	261	6	32	108	71	1	13	524	536	8	-11	104	116	
		4	17	69	43	0	15	179	178	9	-2	704	710	6	33	250	249	1	12	140	150	8	-9	75	85	
		3	19	81	77	0	17	140	140	9	-3	176	175	6	34	379	375	1	11	394	423	8	-8	164	160	
		3	17	93	160	0	18	126	128	9	-4	237	244	6	35	172	171	1	10	59	65	8	-7	130	133	
		3	16	137	126	0	19	107	109	9	-5	184	179	6	36	72	60	1	9	342	366	8	-6	230	231	
		3	15	194	177	0	20	106	106	9	-6	106	106	6	37	148	147	1	8	276	283	8	-5	160	170	
		3	14	216	235	0	21	184	184	9	-7	153	184	6	38	56	39	1	7	107	104	8	-4	164	165	
		3	13	139	139	16	-4	80	47	9	-8	125	110	6	39	167	175	1	6	113	122	8	-3	194	189	
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		3	9	171	183	16	0	159	159	9	-12	69	74	6	42	244	244	1	3	71	78	8	0	374	377	
		3	8	163	185	15	0	163	163	9	-13	145	146	6	43	162	162	1	2	217	207	8	0	211	211	
		3	7	77	76	15	2	136	124	9	-15	71	55	6	44	157	149	1	2	134	135	8	0	191	195	
		3	5	571	593	15	1	176	179	9	-16	119	119	6	45	141	132	1	2	591	699	8	4	192	188	
		3	4	293	316	15	0	81	49	9	-15	94	30	6	46	71	69	1	4	4	91	79	8	7	143	131
		3	3	1195	1167	15	-5	163	151	9	-14	174	182	6	47	87	84	1	4	163	189	8	9	97	109	
		3	2	119	111	15	-7	119	111	9	-11	145	160	6	48	175	182	1	4	195	218	8	5	204	206	
		3	1	606	577	14	-10	76	83	9	-10	177	173	6	49	101	100	1	4	472	467	8	11	112	140	
		3	0	290	290	14	-6	196	188	9	-9	91	74	6	50	147	154	1	4	170	181	8	12	155	162	
		3	-1	804	770	14	-5	94	76	9	-8	79	98	6	51	82	82	1	4	312	325	8	13	85	81	
		3	-2	436	412	14	-4	145	139	9	-6	296	296	6	52	69	91	1	4	289	300	7	11	274	291	
		3	-3	395	345	14	-3	82	96	9	-5	298	305	6	53	75	92	1	4	267	269	7	10	133	122	
		3	-4	828	792	14	-2	77	91	9	-4	178	199	6	54	72	62	1	4	204	212	7	9	314	335	
		3	-5	149	132	14	-1	113	107	9	-3	169	161	6	55	163	164	1	4	108	102	7	8	344	329	
		3	-6	340	331	14	0	113	113	9	-1	242	238	6	56	244	259	1	4	9	75	7	7	223	215	
		3	-7	216	211	14	4	153	141	9	0	100	102	6	57	119	125	1	4	7	112	100	7	6	342	349
		3	-8	198	211	14	5	99	98	9	0	226	231	6	58	558	546	1	4	167	149	7	5	204	206	
		3	-9	142	97	14	6	195	192	9	0	116	111	6	59	99	94	1	4	140	152	7	3	251	237	
		3	-10	77	59	14	8	176	180	9	0	73	74	6	60	753	729	0	3	171	172	7	2	54	18	
		3	-11	63	49	14	10	107	182	9	0	446	494	6	61	551	539	0	3	77	104	7	1	170	187	
		3	-12	249	255	13	9	88	78	9	0	592	603	6	62	186	178	0	3	332	329	7	-1	184	187	
		3	-13	292	288	13	6	144	161	9	0	351	358	6	63	976	918	0	3	474	495	7	-5	160	146	
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		3	-15	169	152	13	0	157	148	9	0	174	172	6	65	423	434	0	3	215	227	7	-9	281	284	
		3	-16	159	147	13	2	103	81	9	0	89	99	6	66	136	138	0	3	354	378	7	-10	74	88	
		3	-17	185	170	13	1	143	136	9	0	83	87	6	67	185	185	0	3	185	185	7	-11	94	73	
		3	-18	134	135	13	-1	251	259	9	0	129	119	6	68	254	269	0	3	171	192	7	-12	197	204	
		3	-19	343	343	13	-3	205	210	9	0	120	98	6	69	77	76	0	3	147	176	7	-13	167	169	
		3	-20	129	128	13	-6	105	102	9	0	177	70	6	70	109	195	0	3	16	92	6	-14	277	270	
		3	-21	110	113	13	-11	110	74	9	0	195	197	6	71	213	220	0	3	213	220	6	-13	150	155	
		3	-22	56	54	13	-12	93	81	9	0	155	209	6	72	254	263	0	3	12	86	6	-12	102	86	
		3	-23	259	259	12	-10	82	92	9	0	193	185	6	73	83	72	14	-2	107	93	6	-11	187	201	
		3	-24	532	516	12	-9	78	54	9	0	150	140	6	74	14	130	14	0	138	156	6	-9	150	150	
		3	-25	495	486	12	-8	173	170	9	0	111	66	6	75	15	90	82	14	0	138	156	6	-9	150	150
		3	-26	749	733	12	-7	77	78	9	0	121	119	6	76	124	121	13	6	101	88	6	-8	74	88	
		3	-27	78																						

Table 2. Continued.

L	H	L	H	L	H	L	H	L	H	L	H	L	H	
K= 6		0	7	190	182	7	11	73	75	2	-2	142	141	
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		0	9	129	124	7	14	116	126	2	-5	229	231	
		0	10	95	166	6	13	266	269	2	-6	135	146	
		0	9	103	103	6	11	221	222	2	-7	122	126	
		0	12	154	147	6	10	123	126	2	-8	95	103	
		0	13	102	121	6	9	140	134	2	-9	353	347	
		0	14	219	219	6	8	171	167	2	-11	88	76	
		0	15	138	127	6	7	238	238	2	-12	176	191	
		0	16	112	108	6	5	379	374	2	-13	162	115	
		0	17	102	101	6	1	261	262	1	-14	141	159	
		0	15	138	127	6	2	198	197	1	-14	135	129	
		0	15	102	101	6	-3	360	374	1	-12	100	99	
		0	13	108	113	6	-1	172	175	1	-11	65	104	
		0	13	82	93	6	-6	139	139	1	-9	222	228	
		0	12	174	141	6	-7	163	165	1	-7	55	51	
		0	13	4	105	112	6	-8	123	118	1	-6	529	541
		0	13	5	100	114	6	-9	116	106	1	-5	57	65
		0	12	7	141	129	6	-10	121	119	1	-4	275	298
		0	12	6	77	33	6	-11	172	175	1	-3	159	137
		0	12	5	180	161	6	-12	104	94	1	-2	194	204
		0	12	5	100	114	6	-13	133	123	1	2	616	625
		0	12	5	100	114	6	-15	117	125	1	3	130	151
		0	12	5	100	114	6	-16	179	176	1	4	347	376
		0	12	5	100	114	6	-17	102	74	1	5	80	49
		0	12	5	100	114	6	-18	326	331	1	6	211	221
		0	12	5	100	114	6	-19	182	176	1	10	194	196
		0	12	5	100	114	6	-20	140	133	1	12	328	323
		0	12	5	100	114	6	-21	203	215	1	14	113	103
		0	12	5	100	114	6	-22	15	8	1	15	8	26
		0	12	5	100	114	6	-23	5	-6	1	15	8	26
		0	12	5	100	114	6	-24	5	-6	1	15	8	26
		0	12	5	100	114	6	-25	5	-6	1	15	8	26
		0	12	5	100	114	6	-26	5	-6	1	15	8	26
		0	12	5	100	114	6	-27	5	-6	1	15	8	26
		0	12	5	100	114	6	-28	5	-6	1	15	8	26
		0	12	5	100	114	6	-29	5	-6	1	15	8	26
		0	12	5	100	114	6	-30	5	-6	1	15	8	26
		0	12	5	100	114	6	-31	5	-6	1	15	8	26
		0	12	5	100	114	6	-32	5	-6	1	15	8	26
		0	12	5	100	114	6	-33	5	-6	1	15	8	26
		0	12	5	100	114	6	-34	5	-6	1	15	8	26
		0	12	5	100	114	6	-35	5	-6	1	15	8	26
		0	12	5	100	114	6	-36	5	-6	1	15	8	26
		0	12	5	100	114	6	-37	5	-6	1	15	8	26
		0	12	5	100	114	6	-38	5	-6	1	15	8	26
		0	12	5	100	114	6	-39	5	-6	1	15	8	26
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		0	12	5	100	114	6	-105	5	-6	1	15	8	26
		0	12	5	100	114	6	-106	5	-6	1	15	8	26
		0	12	5	100	114	6	-107	5	-6	1	15	8	26
		0	12	5	100	114	6	-108	5	-6	1	15	8	26
		0	12	5	100	114	6	-109	5	-6	1	15	8	26
		0	12	5	100	114	6	-110	5	-6	1	15	8	26
		0	12	5	100	114	6	-111	5	-6				

eter shifts were less than 16 % of their corresponding standard deviations. The R -value was now 0.043.

The decrease in the R -value from 0.049 to 0.043 was shown, using the Pawley (1970)¹⁵ simplification of the method proposed by Hamilton,¹⁶ to be significant with a probability greater than 99 %. The R -ratio is 1.140 and should be compared with the calculated ratio $R_{56, 2777, 0.01} = 1.015$. The indices 56, 2777 and 0.01 refer to the dimension of the hypothesis, the number of degrees of freedom, and the significance level, respectively.

A final difference Fourier map was calculated and no abnormalities could be detected in it. Lists of the final positional and thermal parameters are given in Tables 1a and 1b. The observed and calculated structure factors are given in Table 2.

DESCRIPTION AND DISCUSSION OF THE STRUCTURE

The coordination around the copper atom is a distorted octahedron. One bond is formed to the oxygen [O(5)] of the water molecule, and *trans* to it is a bond to an oxygen [O(3)] of a sulphate group. The remaining four bonds are to nitrogens of the imidazole rings and to an oxygen [O(2)] in a second, symmetry-related sulphate group. Thus infinite chains are formed with the sulphate group bridging successive copper atoms (Fig. 2). The chains run in the b -direction along the two-fold screw axes. The symmetry-related chains are held together by hydrogen bonds and van der Waals forces.

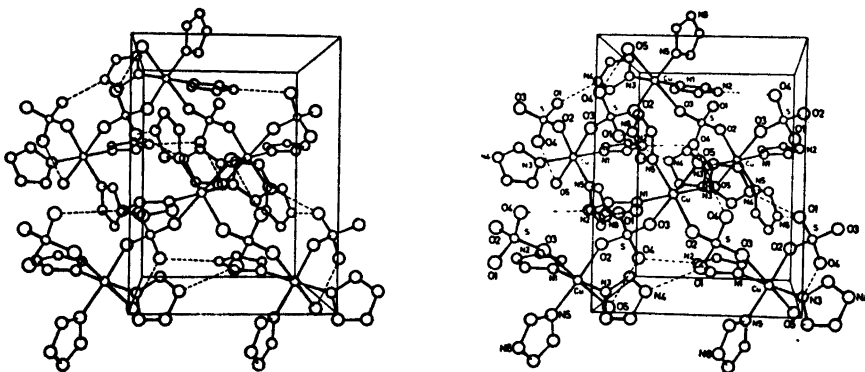


Fig. 2. A stereoscopic illustration of the molecular packing of $[\text{Cu}(\text{H}_2\text{O})(\text{C}_3\text{H}_4\text{N}_2)_3\text{SO}_4]$, viewed along the a -axis. The parenthesis around the numbers are omitted in the figure.

Table 3. Bond lengths and bond angles, and their estimated standard deviations, for the atoms around copper.

Bond length (Å)		Angle (°)	
Cu—N1	1.999(3)	N1—Cu—N3	178.1(1)
Cu—N3	2.002(3)	N5—Cu—O2	176.7(1)
Cu—N5	1.995(3)	O3—Cu—O5	177.6(1)
Cu—O2	2.015(2)	N1—Cu—N5	89.9(1)
Cu—O3	2.578(2)	N5—Cu—N3	91.4(1)
Cu—O5	2.478(3)	N1—Cu—O2	88.2(1)
		N3—Cu—O2	90.6(1)
		O2—Cu—O3	88.1(1)
		O3—Cu—N5	89.2(1)
		O2—Cu—O5	93.0(1)
		N5—Cu—O5	89.9(1)
		O3—Cu—N1	90.2(1)
		O3—Cu—N3	91.2(1)
		O5—Cu—N1	92.0(1)
		O5—Cu—N3	86.7(1)

The coordination around copper. The copper atom is surrounded by three nitrogens and three oxygens. The arrangement is shown in Fig. 1 and distances and angles are given in Table 3. The mean of the three equatorial bond lengths for Cu—N is 1.999(3) Å, which is normal.¹⁻⁵ All the Cu—N bonds are within two standard deviations of this value. The fourth equatorial bond Cu—O(2) is 2.015(2) Å long. Of the three imidazole rings one ring is almost coplanar with the coordination plane around copper (counting the atoms N(1), N(3), N(5), O(2), and Cu), one is almost perpendicular to that plane and the third deviates about 45°. Apparently this does not produce any significant differences in the copper-nitrogen bond lengths. The apical bond

length Cu—O(3) is 2.578(3) Å, which is in good agreement with a recent determination³ [2.574(4) Å] for a bond between copper and a sulphate oxygen, but much longer than the average 2.41 Å in the same kind of bond in CuSO₄·5H₂O.¹⁷ The other apical bond Cu—O(5) is 2.478(3) Å long, which is in good agreement with the range for a copper-water oxygen separation tabulated by Blount *et al.*,¹⁸ but much longer than the 2.19 Å found in (NH₄)₂Cu(SO₄)₂·6H₂O,¹⁹ where water oxygens are also in the apical positions in the coordination octahedron around copper. With these four short and two long bond distances the octahedron is seen to be distorted as expected.²⁰ The octahedron is also angularly distorted which is shown from significant differences for almost all of the angles compared to the ideal ones. The greatest difference is 3.3(1)° [O(5)—Cu—N(3)].

The sulphate group. In the sulphate group the oxygens are arranged in a tetrahedron which is nearly ideal, although three of the six tetrahedral angles differ significantly from the ideal one. The deviations are 1.7(2)° for [O(1)—S—O(2)]; 0.9(2)° for [O(1)—S—O(3)], and 1.0(2)° for [O(2)—S—O(3)]. The differences in sulphur-oxygen bond lengths do not seem to depend on whether the oxygen atoms are coordinated to a copper atom or not.

Bond distances and angles are given in Table 4. The sulphur-oxygen bond distances are in good agreement with those given in the recent tabulation by Andreotti, Cavalca and Musatti.²¹

Water and hydrogen bonds. The distances of the water hydrogens to the water oxygens are 0.96(6) Å for H(13) and 0.87(6) Å for H(14). This is longer than expected when a comparison is made with similar bonds in MoO₃·2H₂O,²² where the range of distances in sixteen O—H

bonds is 0.69(5)—0.84(5) Å, considering that both determinations are from X-ray data. The O—H distances in CuSO₄·5H₂O¹⁷ calculated from neutron diffraction data have a mean value of 0.96 Å and our values should therefore show a reasonable shortening of at least 0.1 Å.²³

It seems possible that the distances found in this determination depend on the oxygen coordination to copper and the two hydrogen bonds formed to sulphate oxygens. These hydrogen bond lengths are [O(4)···H(13)—O(5)] = 2.813(4) Å and [O(4)···H(14)—O(5)] = 2.776(4) Å and the deviation of the bonds is such that the angle H(13)—O(5)—H(14) is 97 (5)° which is smaller than those in MoO₃·2H₂O [mean value 109(6)°].

The hydrogen atoms on the imidazole nitrogens also take part in a hydrogen bonding scheme. The acceptor atoms are sulphate oxygens which are not copper-coordinated. Hydrogen bonds within the symmetry-related chains are [N(2)—H(4)···O(4)] = 2.847(4) Å, [N(4)—H(8)···O(1)] = 2.871(4) Å and [O(5)—H(14)···O(4)] = 2.776(4) Å. Those between the chains are [N(6)—H(12)···O(1)] = 2.762(4) Å and [O(5)—H(13)···O(4)] = 2.813(4) Å. No significant difference of the hydrogen bond distances between N—O and O—O can be seen. All hydrogen bond lengths are of the same magnitude as those found in similar structures.^{3,4}

The imidazole rings. Interatomic distances and angles for the imidazole rings are given in Table 5. Considering the standard deviations there are no significant differences in the bond distances and angles for the three rings. Bond distances and angles between carbons and nitrogens are also about the same as those found in other structure determinations.¹⁻⁵ The bond distance range for hydrogens to carbons and nitrogens is 0.81(5) Å to 0.96(5) Å. Planes through the positions of the nitrogen and carbon atoms in respective imidazole rings were calculated and have the equations

1. $0.2334x + 0.0764y - 0.9694z + 0.2486 = 0$
[N(1), N(2), C(1), C(2), C(3)]
2. $0.7265x - 0.4784y - 0.4933z + 1.7762 = 0$
[N(3), N(4), C(4), C(5), C(6)]
3. $-0.4940x - 0.8414y - 0.2192z - 3.4449 = 0$
[N(5), N(6), C(7), C(8), C(9)]

The maximum deviations of non-hydrogen atoms from the planes are 0.001 Å, 0.004 Å, and 0.003 Å for the first, second, and third imidazole

Table 4. Bond lengths and bond angles, and their estimated standard deviations, for the sulphate group.

Bond lengths (Å)		Angle (°)	
S—O1	1.473(3)	O1—S—O2	107.8(2)
S—O2	1.480(3)	O1—S—O3	110.4(2)
S—O3	1.457(3)	O1—S—O4	109.5(2)
S—O4	1.489(3)	O2—S—O3	110.5(2)
		O2—S—O4	109.3(2)
		O3—S—O4	109.5(2)

Table 5. Bond lengths and bond angles, and their estimated standard deviations, for the imidazole rings.

Bond length (Å)		Angle (°)	
N1-C1	1.313(5)	C3-N1-C1	105.9(3)
N1-C3	1.367(5)	N1-C1-N2	110.7(3)
N2-C1	1.337(5)	C1-N2-C2	107.8(3)
N2-C2	1.357(6)	N2-C2-C3	106.1(3)
C2-C3	1.347(6)	C2-C3-N1	109.5(3)
N3-C4	1.321(5)	C6-N3-C4	105.0(3)
N3-C6	1.381(5)	N3-C4-N4	111.5(3)
N4-C4	1.337(5)	C4-N4-C5	107.3(3)
N4-C5	1.369(5)	N4-C5-C6	106.3(4)
C5-C6	1.342(6)	C5-C6-N3	109.9(3)
N5-C7	1.319(5)	C9-N5-C7	106.7(3)
N5-C9	1.377(5)	N5-C7-N6	110.2(3)
N6-C7	1.340(5)	C7-N6-C8	108.2(3)
N6-C8	1.361(6)	N6-C8-C9	106.4(3)
C8-C9	1.358(6)	C8-C9-N5	108.6(3)
H1-C1	0.94(5)	H1-C1-N1	127.1(32)
H2-C2	0.92(6)	H1-C1-N2	122.2(32)
H3-C3	0.94(5)	H2-C2-N2	122.2(41)
H4-N2	0.81(5)	H2-C2-C3	131.5(40)
H5-C4	0.89(5)	H3-C3-N1	119.1(28)
H6-C5	0.95(5)	H3-C3-C2	131.2(28)
H7-C6	0.96(5)	H4-N2-C1	128.8(36)
H8-N4	0.90(5)	H4-N2-C2	123.4(36)
H9-C7	0.96(5)	H5-C4-N3	121.2(34)
H10-C8	0.95(5)	H5-C4-N4	126.7(34)
H11-C9	0.87(4)	H6-C5-N4	126.4(33)
H12-N6	0.92(5)	H6-C5-C6	127.2(34)
		H7-C6-C5	128.6(26)
		H7-C6-N3	121.4(26)
		H8-N4-C4	122.3(31)
		H8-N4-C5	130.1(31)
		H9-C7-N5	124.9(29)
		H9-C7-N6	124.4(29)
		H10-C8-N6	122.2(33)
		H10-C8-C9	131.4(33)
		H11-C9-C8	128.0(30)
		H11-C9-N5	123.2(29)
		H12-N6-C7	122.5(29)
		H12-N6-C8	129.2(29)

rings, respectively. The corresponding maximum deviations of hydrogens are 0.06 Å [H(3)], 0.12 Å [H(5)], and 0.11 Å [H(9)] Å, respectively. None of these hydrogen atoms is involved in hydrogen bonds.

Conclusions. This structure determination has shown that when the anion is sulphate and the ratio of imidazole to copper is 3:1 the coordination around copper in the equatorial plane is formed by three imidazole nitrogens and a sulphate oxygen. The water molecule can thus not compete with the oxygen of the anion. We think that the systematic change of anions and

different ratios of imidazole to copper will show (as described in the introduction) differences in coordination of the anions to copper. This in turn will provide us with more variations in copper-imidazole interactions than has hitherto been found.

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