The Crystal Structure of $(Mo_{03}V_{07})_2O_5$ of R-Nb₂O₅ type and a Comparison with the Structures of V_2O_5 and V_2MoO_8

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 $(Mo_{0.3}V_{0.7})_2O_5$ represents the molybdenum rich limit (at 650°C) of a range of solid solution extending from V_2O_5 along the line $(Mo_xV_{1-x})_2O_5$ in the Mo-V-O system. There are, however, discontinuities within this range associated with symmetry changes. This phase has been studied by single crystal diffraction methods. The dimensions of the monoclinic unit cell are a=11.809 Å, b=3.652 Å, c=4.174 Å, $\beta=90.56°$, and the space group is C2.

c=4.174 Å, $\beta=90.56^\circ$, and the space group is C2. The structure is of the same type as that of $R\text{-Nb}_2\mathrm{O}_5$ and can be considered as composed of $M\mathrm{O}_6$ octahedra coupled in the same way as in $\mathrm{V}_2\mathrm{O}_5$, although the distortion of the metal atoms within the octahedra follows a different pattern. This distortion, as reflected in the considerable divergence of the $M-\mathrm{O}$ bond lengths, is intermediate in magnitude between that in $\mathrm{V}_2\mathrm{O}_5$ and MoO_3 . Molybdenum and vanadium atoms are randomly distributed over the metal atom positions.

The structure is also closely related to that of V₂MoO₈.

In the course of an investigation of the phases formed in the system $V_-Mo_-O^1$ it has been observed that molybdenum may replace vanadium in V_2O_5 . This replacement gives rise to a range of solid solution, $(Mo_xV_{1-x})_2O_5$, extending at 650°C to the composition $(Mo_{0.3}V_{0.7})_2O_5$ approximately. To a first approximation the unit cell dimensions vary gradually within this interval but a closer examination of the powder patterns and comparison with single crystal photographs revealed that the symmetry has changed from orthorhombic for V_2O_5 to monoclinic for $(Mo_{0.3}V_{0.7})_2O_5$. According to preliminary results, this transition occurs at a composition of about x=0.20 and is probably associated with the occurrence at this composition of a phase giving a more complex powder pattern. Further studies of these problems are in progress.

This article presents a structure determination of a crystal with a composition close to the molybdenum-rich limit. A short communication of the investigations reported below was given at the Seventh International Congress of Crystallography.²

EXPERIMENTAL

The crystal studied was selected from a sample prepared by heating a mixture of MoO_3 , V_2O_5 , and V_2O_3 of gross composition $Mo_{0.3}V_{0.7}O_{2.5}$ in a sealed silica tube at 650°C for 2 days. The powder pattern of this sample showed the lines (Table 1) of a phase which for 2 days. The powder pattern of this sample showed the lines (Table 1) is phase which could be indexed on the basis of a monoclinic unit cell with the dimensions given in Table 2. A few additional weak lines could be assigned to VOMoO₄³ and it seems therefore probable that the monoclinic phase contained slightly less molybdenum than indicated by the gross composition and that its formula should be approximately $(Mo_{0.28}V_{0.72})_2O_5$.

The crystal was shaped like a somewhat truncated parallelepiped with the dimensions 0.0204 mm (along a), 0.0636 mm (along b), and 0.0053 mm (along c). Integrated Weissenberg photographs were recorded of the hOt by and hOt layer lines using CuKg radiation

berg photographs were recorded of the h0l, h1l and h2l layer lines using $CuK\alpha$ radiation and multiple film technique. The relative intensities of the reflections were measured by

Table 1. X-Ray powder diffraction data for $(Mo_{0.3}V_{0.7})_2O_5$, $CuK\alpha_1$ radiation $(\lambda=1.54051$ Å).

I	$d_{ m obs}$	$\sin^2\! heta_{ m obs}$	hkl	$(\sin^2\theta_{\rm obs} - \sin^2\theta_{\rm calc})$
	Å	$\times 10^{5}$		× 10 ⁵
		,,		• • • • •
w	5.894	1708	200	+ 6
$\mathbf{w} +$	4.169	3414	001	i 9
\mathbf{st}	3.487	4878	110	+ 5
w	3.419	5074	$\overline{2}01$	+14
w	3.392	5157	201	+ 2
$\mathbf{w}+$	2.952	6810	400	+ 3
			(111	+32
\mathbf{st}	2.678	8270	{ 3 10	– 7
			(<u>1</u> 11	-16
vw	2.420	10131	$\overline{4}01$	+13
vw	2.087	13621	002	0
w	1.9685	15311	600	- 6
vw	1.9638	15384	$\boldsymbol{202}$	-34
\mathbf{m}	1.8270	17775	020	15
w	1.7980	18353	$\overline{5}11$	17
w	1.7944	18426	$\bar{1}12$	-20
$\mathbf{v}\mathbf{w}$	1.7458	19466	220	-26
vw	1.7117	20250	$\overline{4}02$	+12
\mathbf{w}	1.6738	21178	021	-17
\mathbf{w}	1.6086	22927	221	-18
$\mathbf{w} +$	1.5533	24589	420	– 9
\mathbf{m}	1.5316	25293	<u>7</u> 10	_ 2
$\mathbf{v}\mathbf{w}$	1.4583	27898	$\overline{4}21$	-10
\mathbf{w}	1.4438	28461	$\overline{5}12$	—_7
$\mathbf{v}\mathbf{w}$	1.4415	28551	711	+17
\mathbf{m}	1.3386	33110	620	+ 3
\mathbf{w}	1.2722	36659	621	$+$ $\underline{4}$
vw	1.2541	37724	<u>4</u> 03	-15
vw	1.2488	38046	$\frac{1}{4}22$	+17
vw	1.2109	40460	∫802	-11
• • • •	1.2100	10100	130	$+ _{-6}$
vw	1.1809	42545	/911	+17
* **	111000	12010	10,0,0	- 1
w	1.1633	43841		$+ \frac{6}{10}$
			(330	-16
vw	1.1235	47000	622	-13
vw	1.1214	47175	331	-16
vw	1.1197	47325	331	- 9

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means of a densitometer. These values were corrected for the effect of absorption (crystal assumed to be bounded by 7 planes; $\mu=496~\rm cm^{-1}$) and the usual Lp-correction was applied. These calculations as well as the subsequent structure factor calculations, least squares refinement and calculations of interatomic distances were performed on a computer of type FACIT EDB by means of the programs No. 6015, 6016, 6019, 6023, and 6030 4 (the Lp-program written by B. Lundberg is not listed in Ref. 4). The atomic scattering factors listed in International Tables 5 were used, namely, for neutral oxygen and vanadium the values given in Table 3.3.1 A and for molybdenum those given in Table 3.3.1 B. The real part of the dispersion correction 5 was applied to these values.

DETERMINATION AND REFINEMENT OF THE STRUCTURE

Systematic extinction was observed for all reflections hkl with h + k = 2n + 1. Together with the observed Laue symmetry 2/m this led to the three possible space groups C2/m (No. 12), C2 (No. 5), and Cm (No. 8).

The fact that the crystal under investigation represented one end of a range of solid solution (cf. above) the other limit of which is V_2O_5 suggested a close relationship between the crystal structures. The space group of V_2O_5 is Pmnm (No. 59)^{6,7} or possibly $Pmn2_1$ (No. 31)⁷ which, on the other hand, implies a basic difference between the two structures.

A model was tried in which the arrangement of MO_6 octahedra was the same as in V_2O_5 but in which the distortion of the metal atoms from the centres of these octahedra was different to account for the different symmetry. Structure factor calculations and least squares refinement proved this model to be correct. The structure is shown in Fig. 1 together with that of V_2O_5 . Completely random distribution of molybdenum and vanadium atoms over the metal atom positions had to be assumed since these positions were crystallographically equivalent and no indication of a superstructure had been observed on the X-ray photographs. Because of the uncertainty in the exact composition of the crystal (cf. above) three different Mo:V ratios were tested, viz. M = (0.33 Mo + 0.67 V), (0.30 Mo + 0.70 V), and (0.27 Mo + 0.73 V). The results, obtained by least squares refinement, differed only insignificantly, however.

The space group Cm was hardly consistent with the structure model but the remaining two, C2/m and C2, were both possible. Least squares refinement was carried out for both alternatives, namely (I) 1 M and 2 O in positions 4i, and 1 O in 2a of space group C2/m and (II) 1 M and 2 O in 4c and 1 O in 2a of space group C2. The final R-values (based on observed reflections only) were about the same for both alternatives, viz. 0.071 and 0.070, respectively, but the final y coordinates of O(1) and O(2) in alternative II differed by 7.0σ and 5.1σ , respectively, (σ = the corresponding standard deviation) from the values 0 and $\frac{1}{2}$ at which they are fixed by symmetry in alternative I. The temperature factors obtained were also less divergent in alt. II than in alt. I and, particularly, they were much lower for atoms O(1) and O(2) in alt. II. It was thus evident that the structure is best described in the non-centrosymmetric space group C2 and the final parameters for this case are given in Table 2.

Weights in the least squares procedure were calculated according to Cruickshank's formula, $w = 1/(A + F_o + C \cdot F_o^2)$, where the following values were chosen for the parameters, A = 18, C = 0.012. The final weight analysis

is given in Table 3. The observed and calculated structure factors are listed in Table 4.

Table 2. The crystal structure of $(Mo_{0.3}V_{0.7})_2O_5$.

Space-group: C2 (No.5) Unit cell dimensions:* $a=11.809~(\pm~2)~\text{\AA}$ $b=~3.652~(\pm~1)~\text{Å}$ $c=~4.174~(\pm~1)~\text{Å}$ $\beta=~90.56~(\pm~2)~^\circ$

Unit cell content: 2 M_2O_5 , $M = (Mo_{0.28}V_{0.72})$, Mo/V ratio approximative (see text).

Atom	Position	$x \pm \sigma(x)$	$y \pm \sigma(y)$	$z \pm \sigma(z)$	$B \pm \sigma(B)$	
M		0.14892 ± 0.00025	0	0.10034 ± 0.00076		
O(1) O(2) O(3)		$egin{array}{ccc} 0.1446 & \pm & 0.0015 \ 0.1792 & \pm & 0.0013 \ 0 & 0 & 0 \end{array}$		$ \begin{vmatrix} 0.4934 & \pm 0.0042 \\ 0.9953 & \pm 0.0037 \\ 0 \end{vmatrix} $	$egin{array}{cccc} 1.09 & \pm 0.32 \ 0.51 & \pm 0.26 \ 1.73 & \pm 0.47 \end{array}$	

^{*} $a[KCl, 25^{\circ}C] = 6.29228 \text{ Å}.^{13}$

DISCUSSION

The structure of $(Mo_{0.3}V_{0.7})_2O_5$ turns out to be isotypic with that recently suggested by Gruehn for $R\text{-Nb}_2O_5$ on the basis of powder diffraction data.⁶ The unit cell dimensions given for $R\text{-Nb}_2O_5$ are (the a and c axes interchanged here), $a=12.7_9$ Å, $b=3.82_6$ Å, $c=3.98_3$ Å, $\beta=90.7_5$ °. The space group was assumed to be (A2/m=) C2/m and the following atomic coordinates were reported (the numbering of the atoms changed here to become analogous with that in Table 2).

Table 3. Weight analysis obtained in the last cycle of refinement. $\Delta = ||F_{\text{obs}}| - |F_{\text{calc}}||$, w = weighting factor. The $\overline{w\Delta^2}$ values have been normalized.

$\begin{array}{c} \textbf{Interval} \\ \textbf{sin } \theta \end{array}$	Number of independent reflections	$\overline{w \it \Delta^2}$	$\frac{ \text{Interval}}{ F_{\text{obs}} }$	Number of independent reflections	$\overline{w arDelta^2}$
$\begin{array}{c} 0.00-0.46 \\ 0.46-0.58 \\ 0.58-0.67 \\ 0.67-0.74 \\ 0.74-0.79 \\ 0.79-0.84 \\ 0.84-0.89 \\ 0.89-0.93 \end{array}$	26 21 15 15 13 11 10	0.71 0.84 1.49 0.82 0.51 1.20 0.99 1.28	$\begin{array}{c} 0-16 \\ 16-24 \\ 24-32 \\ 32-40 \\ 40-48 \\ 48-56 \\ 56-64 \\ 64-72 \end{array}$	3 7 29 32 19 18	0.47 1.75 1.19 1.11 1.04 0.60 0.86 0.76
$\begin{array}{c c} 0.89 - 0.93 \\ 0.93 - 0.97 \\ 0.97 - 1.00 \end{array}$	15 6	$0.82 \\ 2.94$	>72	10	0.73

	$oldsymbol{x}$	$oldsymbol{y}$	\boldsymbol{z}
Nb	0.146	0	0.07
O(1)	0.16	0	0.5
O(2)	0.18	0.5	0
O(3)	0	0	0

A comparison with Table 2 emphasizes the similarity between the two structures. The discussion below, therefore, applies also to R-Nb₂O₅.

The coordination of oxygen atoms around vanadium in V_2O_5 may be described either as five- or sixfold since the sixth V-O bond is considerably longer than the other five.^{7,8} If the coordination is regarded as six-fold the structure may be described as built up of octahedra sharing edges and corners as visualized in Fig. 1 b. Comparison with Fig. 1 a indicates that the coupling of the octahedra is the same in $(Mo_{0.3}V_{0.7})_2O_5$. The structures can thus be described as built of edge sharing octahedra which form zig-zag chains that run in the b direction. These chains are mutually connected by corner sharing between octahedra in adjacent chains. Alternatively, they may be regarded as consisting of slabs of ReO_3 -type, two octahedra thick, which extend infinitely in the bc plane; these, in turn, are interconnected by edge-sharing between

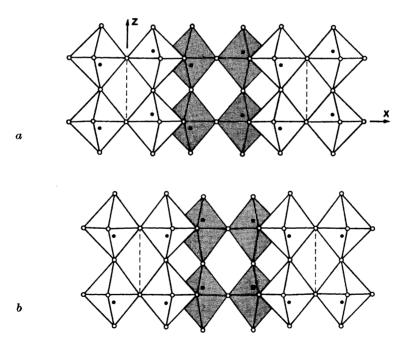


Fig. 1. The structures of (a) $(Mo_{0.3}V_{0.7})_2O_5$ and (b) V_2O_5 visualized as built up of MO_6 octahedra at two levels (light and shaded, respectively). These polyhedra share corners with crystallographically identical ones above and below. The positions of the metal inside the octahedra are indicated by dots.

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Table 4. Observed and calculated structure amplitudes and calculated phase angles (expressed as a fraction of one cycle). $\Delta = ||F_{\rm obs}| - |F_{\rm calc}||$. The values of $\Delta \sqrt{w}$ have been normalized.

<u>h</u>	<u>k</u>	ļ	Fobe	Fcalc	∆√w	α	<u>h</u>	ķ	1	Pobs	Foalc	∆ √w	α
26260244400484248026822220862024680424680424824680209551555111111111115555555	1111111111111111111	<u>^^^^^^^000000000000000000000000000000</u>	338640946697833392472942375984051989641566215013415541166725731853411837 98270124540273037604441524452 98270124540275055577774524528658215257555548355655224500255224232555342555225532658	46663457078440873667551847945860420022752302906845521230784791596798578671865155235455278655184791596798578	41558915008918445289110889322444550897614410071415069594502570000000000000000000000000000000000	0.00000 0.50000	5579991133117315711197513590862260002224444666688800022218642086420246286		0.51401501000011111000000555555555555555	27.0 #0860713918#93951921#61301926071906201935#3#9#5518#32#236935#80##2251555#62072078669#575588#61271551776601112201935#44#75574062076227651777663772275527766112205147#4#75574062076227651777663742250	2063695807769478772124341823509713906817711745574449338719960224834 22977835551063807769478772124345867755512725099345241139068177117455744449338719960224834 237785557448186777594434677555127250993452411390681771174557444493387199602248374	0611742608285924247880005677219422752666587429322605677829416000010000000000000000000000000000000	0.01328 0.004694 0.004694 0.004694 0.004694 0.004694 0.004694 0.004694 0.00566621 0.0056621 0.0056621 0.0062862

component octahedra. The latter is a description in terms of a shear structure ontroduced by Magnéli on and later developed by Andersson. The difference between the two structures becomes significant when the

The difference between the two structures becomes significant when the distortions of the metal atoms from the centres of the octahedra are considered. These displacements occur predominently along the direction of the c axis.

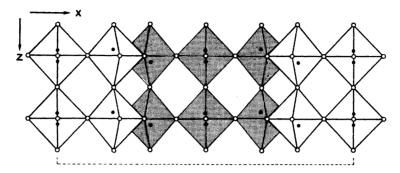


Fig. 2. The structure of V_2MoO_8 presented analogously with those in Fig. 1. In the octahedra containing two dots the metal atoms are situated alternatingly at the two positions in the strings of octahedra running along the line of sight. The dashed line indicates a repeat distance.

It is seen in Fig. 1 that in V_2O_5 all metal atoms within an ReO_3 -type slab are displaced in the same direction while in $(Mo_{0.3}V_{0.7})_2O_5$ they are shifted pairwise in opposite directions. The reason for this interesting difference between the two structures is not understood and is being further investigated. In both structures the metal atoms in a pair of octahedra sharing edges are displaced in opposite directions which, of course, is energetically most favorable from a purely electrostatic point of view.

It is interesting to compare these two structures with that of $V_2MoO_8^{12}$ shown in Fig. 2. Here the slabs of ReO_3 type have a thickness of three octahedra instead of two but the interconnection of the slabs remains the same. Homologous series of structures is a term introduced by Magnéli for this type of structural relationship. Considering the offcenter displacements of the metal atoms V_2MoO_8 forms an intermediate between the above-mentioned structures since the displacement within the middle octahedra of each slab goes in both directions; it alternates between +z and -z when going in the direction of the b axis which is therefore doubled (cf. Fig. 2). Both types of relative displacement within neighboring octahedra are thus present simultaneously in this structure.

Table 5. Metal oxygen distances.

Atoms	$x \qquad \qquad y \qquad z \qquad \qquad z$		Distance (in Å)	$V_2O_5(^8)$ Distance (in Å)	MoO ₃ (14) Distance (in Å)	
M- -O(1) -O(2) -O(3)	0.149 0.145 0.179 0	$0 \\ 0.065 \\ -0.448 \\ 0.002$	$0.100 \\ 0.493 \\ -0.005 \\ 0$	$egin{array}{c} 1.659\ (\pm\ 18) \ 1.733\ (\pm\ 36) \ 1.804\ (\pm\ 3) \end{array}$	1.585 1.780 1.878	1.671 1.734 1.948
-O(2) -O(2) -O(1)	$0.321 \\ 0.179 \\ 0.145$	$0.052 \\ 0.552 \\ 0.065$	$0.005 \\ -0.005 \\ -0.507$	$2.081 (\pm 16) 2.094 (\pm 36) 2.544 (\pm 18)$	1.878 2.021 2.785	1.948 2.251 2.332

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The M-0 distances which are given in Table 5 can be grouped together in three short, two intermediate, and one long bond. There is thus a marked tendency towards five-fold coordination although not as pronounced as in V_2O_5 . The range of the M-O distances is seen to be intermediate between those in V₂O₅ and MoO₃. All close O—O distances have normal values ranging from 2.48 (\pm 6) Å (along the shared edge) to 2.97 (\pm 2) Å.

The Nb-O distances in R-Nb₂O₅ as given by Gruehn 6 range from 1.7 to 2.3 Å which indicates a slightly smaller distortion in that structure than in

the isostructural $(Mo_{0.3}V_{0.7})_2O_5$.

Acknowledgements. The work reported in this article forms a part of a research program sponsored in part by the Swedish Natural Science Research Council and in part by the European Research Office, United States Army, Frankfurt am Main, Germany. Grants for the use of computers were received from the Computer Division of the National Swedish Rationalization Agency (Kungl. Statskontoret).

I am indebted to Professor A. Magnéli for valuable comments on the manuscript.

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Received June 12, 1967.