

## Electrometric Investigation of Equilibria between Mercury and Halogen Ions

### III. The „Millimolar” Potentials of Mercury and the Solubility Product of Mercury (I) Chloride

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In Part I<sup>1</sup> of this series the «millimolar potentials»  $E_{10}$ ,  $E_{1X}$ , and  $E_{20}$  were defined as the emf of the cells

$$-CE / \text{Hg}_2^{2+} / \text{Hg} + \quad E = E_{10} + 29.58 \log (\text{Hg}_2^{2+}) \quad (1)$$

$$-CE / \text{X}^-, \text{Hg}_2\text{X}_2 / \text{Hg} + \quad E = E_{1X} - 59.16 \log (\text{X}^-) \quad (2)$$

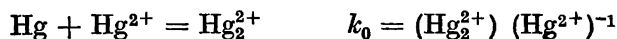
$$-CE / \text{Hg}_2^{2+}, \text{Hg}^{2+} / \text{Pt} + \quad E = E_{20} + 59.16 \log (\text{Hg}^{2+}) - \\ - 29.58 \log (\text{Hg}_2^{2+}) \quad (3)$$

when all concentrations appearing in the expression for  $E$  are 1 mC\*. These millimolar potentials are defined under the special experimental conditions we have chosen: at a temperature of 25° C with  $(\text{H}^+) = 10$  mC and  $(\text{ClO}_4^-) + \text{X}_{\text{total}} = 500$  mC in the right electrode vessel, and with the reference electrode

$$CE = \text{Hg}, \text{Hg}_2\text{Cl}_2 / 4 \text{ C NaCl} / 0.5 \text{ C NaClO}_4 / \quad (4)$$

to the left.

The millimolar emf:s are connected with the equilibrium constant for



\*) C = mole/l; mC = mmole/l.

by the relation

$$E_{20} - E_{10} = 59.16 \log k_0 \quad (5)$$

The solubility products of the  $\text{Hg}_2\text{X}_2$  can be calculated from  $E_{10}$  and  $E_{1x}$  by

$$E_{1x} - E_{10} = 29.58 \log k_s; k_s = (\text{Hg}_2^{2+}) (\text{X}^-)^2 \quad (6)$$

A knowledge of these quantities was necessary for the following calculations on  $\text{Hg}^{2+}-\text{X}^-$  complexes. Now, the four calomel electrodes used — »A», »F», »G» and »I» — had slightly different potentials, as was found for example by direct comparison, connecting them all to a vessel with 4 C NaCl. Moreover these differences varied slightly with time. Accordingly, the values of  $E_{10}$  and  $E_{20}$  also varied slightly.

In order to make measurements at different times and with different CE:s comparable, we »standardized» all emf:s relative to  $E_{10}$ , which was measured every now and then. Where it was necessary a correction was introduced — generally different for the different CE:s — so as to make  $E_{10}$  equal to  $E_{10}^{\#} = 434.5$  mV. These corrections never exceeded 2 mV.

#### TITRATIONS FOR DETERMINING THE REDOX POTENTIAL $E_{20}$

To determine  $E_{20}$ , titrations were made with Pt electrodes, where S (the original solution in the titration vessel) contained  $\text{Hg}_2^{2+}$  and T (the solution added during the titration) contained  $\text{Hg}^{2+}$ . Generally T contained  $\text{Hg}_2^{2+}$  too in the same concentration as in S, which facilitated the calculation. The first point of such a titration, corresponding to the »pure  $\text{Hg}_2^{2+}$ » solution, is rather well defined (within 1 or 2 mV) as there is always a certain amount of  $\text{Hg}^{2+}$  left in a solution prepared by shaking to equilibrium with metallic Hg.

$E_{20}$  and the  $\text{Hg}^{2+}$  correction could be calculated in two ways:

1) An approximate value of  $E_{20}$  was obtained from a point with high ( $\text{Hg}^{2+}$ ); with this  $E_{20}$ , the ( $\text{Hg}^{2+}$ ) in the » $\text{Hg}_2^{2+}$ » solution was calculated. Then a better value of  $E_{20}$  was calculated, and so on.

2) They could also be found by direct calculation. We assume that S contains  $(b - \frac{\delta}{2})$  mC  $\text{Hg}_2^{2+}$  and  $\delta$  mC  $\text{Hg}^{2+}$ , and that T contains  $(b - \frac{\delta}{2})$  mC  $\text{Hg}_2^{2+}$  and  $(a + \delta)$  mC  $\text{Hg}^{2+}$ , where  $a$  and  $b$  are known from the analyses of total Hg content. After addition of  $v$  ml of T to 100 ml of S

$$(\text{Hg}_2^{2+}) = b - \frac{\delta}{2}, (\text{Hg}^{2+}) = \delta + av (100 + v)^{-1}$$

and according to (3)

$$E(v) = E_{20} + 59.16 \log [\delta + av (100 + v)^{-1}] - 29.58 \log (b - \frac{\delta}{2})$$

$$E(0) = E_{20} + 59.16 \log \delta - 29.58 \log (b - \frac{\delta}{2})$$

$$\Delta E = E(v) - E(0) = 59.16 \log [1 + av\delta^{-1} (100 + v)^{-1}] \quad (7)$$

$\delta$  is obtained directly from (7)

The ratio  $(\text{Hg}_2^{2+})/(\text{Hg}^{2+})$  was usually about 100—120 in our » $\text{Hg}_2^{2+}$ » solutions, which is not far from the equilibrium constant  $k_0$  obtained by us (see (18)). It cannot be expected to agree exactly, as the equilibrium was established under very different conditions.

Table 1 gives a typical titration for  $E_{20}$ , showing the validity of (3).

Table 1. Titration for  $E_{20}$ . Pt electrode, CE »G».

$$S = (4.863 - \frac{\delta}{2}) \text{Hg}_3^{2+}, \delta \text{Hg}^{2+}.$$

$$T = (4.863 - \frac{\delta}{2}) \text{Hg}_2^{2+}, (19.47 + \delta) \text{Hg}^{+2}.$$

$v$ ml	$E$ mV	$\delta$ mC	$(\text{Hg}^{2+})$ mC	$E_{20}$ mV
0	458.65		0.0437	
5.00	537.8	0.0446	0.971	(558.8 <sub>2</sub> )
9.97	554.2	0.0439	1.809	559.2 <sub>3</sub>
15.00	563.45	0.0439	2.583	559.3 <sub>3</sub>
20.00	569.7	0.0437	3.289	559.3 <sub>7</sub>
25.00	574.3	0.0437	3.937	559.3 <sub>4</sub>
30.00	578.0	0.0436	4.537	559.4 <sub>0</sub>
35.00	580.95	0.0437	5.092	559.3 <sub>9</sub>
40.03	583.4	0.0437	5.160	559.3 <sub>5</sub>

When  $v$  ml of T had been added the emf was  $E$  mV. From  $E(0)$  and  $E(v)$ ,  $\delta$  was calculated by means of formula (7). If an average value  $\delta = 0.0437$  mC is accepted,  $(\text{Hg}_2^{2+})$  was 4.841 during the entire titration, whereas the calculated values of  $(\text{Hg}^{2+})$  are given in the fourth column. Finally  $E_{20}$  was calculated by means of (3). The mean value (excluding the value at 5.00 ml where a small error in  $v$  causes a large error in  $E_{20}$ ) was  $E_{20} = 559.3_4 \pm 0.1$  mV (not standardized).

#### THE MERCURY ELECTRODE IN $\text{Hg}_2^{2+} - \text{Hg}^{2+}$ SOLUTIONS

When a Hg electrode and a solution containing  $\text{Hg}_2^{2+}$  and  $\text{Hg}^{2+}$  are in equilibrium in accordance with (4),  $E$  can equally well be expressed by (1) or by (3), as in this case the Hg can also be regarded as a redox electrode. One might of course also use the expression for a  $\text{Hg}^{2+}/\text{Hg}$  electrode, which is easily derived from (1) and (3):

$$- \text{CE} \parallel \text{Hg}^{2+} \mid \text{Hg} + ; E = \frac{1}{2} (E_{10} + E_{20}) + 29.58 \log (\text{Hg}^{2+}) \quad (8)$$

For the following investigation it was of interest to know how a Hg electrode would behave in solutions where the concentrations of  $\text{Hg}_2^{2+}$  and  $\text{Hg}^{2+}$  do not correspond to equilibrium with Hg. One might imagine that the emf would in such cases, depending on the rate of the different relevant reactions, be determined principally by the concentration of  $\text{Hg}_2^{2+}$  (1), or by that of  $\text{Hg}^{2+}$  (8), or that Hg would act chiefly as a redox electrode (3). Actually none of these was found to be the case.

To settle the question, a titration was made with both Hg and Pt electrodes, where S contained 4.93 mC  $\text{Hg}_2^{2+}$  and 0.05 mC  $\text{Hg}^{2+}$ , and T contained 5.00 mC  $\text{Hg}^{2+}$ . After equilibrium the concentration of  $\text{Hg}_2^{2+}$  should therefore be practically unchanged. The results are shown in Table 2. With the first small additions,  $E_{\text{Hg}}$  scarcely changed at all and even after adding 55 ml, so that  $(\text{Hg}_2^{2+}) \approx$

Table 2. Mercury electrode in  $\text{Hg}_2^{2+} - \text{Hg}^{2+}$ .  
*S* = 4.93  $\text{Hg}_2^{2+}$  0.05  $\text{Hg}^{2+}$ , *T* = 5.00  $\text{Hg}^{2+}$ .

<i>v</i> ml	<i>t</i>	$E_{\text{Hg}}$	$E_{\text{Pt}}$
0		454.55	(~455)
2	3m	454.5	
	6m	»	
	10m	»	
5	5m	454.45	
	10m	454.5	
	16m	»	
15	10m	454.45	
	15m	454.5	
35	10m	454.3	
55	5m	454.15	556.25
	16m	454.1	555.3
	21m	»	554.95
	25m	»	554.6
	72m	454.4	550.45
	104m	454.35	546.35
	144m	»	543.75
	24h	454.45	508.7
36h	454.5	500.8	

The times *t* are counted from the last addition of T. For each value of *v* the last *E* was always read immediately before the next addition of T.  $E_{\text{Hg}}$  and  $E_{\text{Pt}}$  are not standardized.

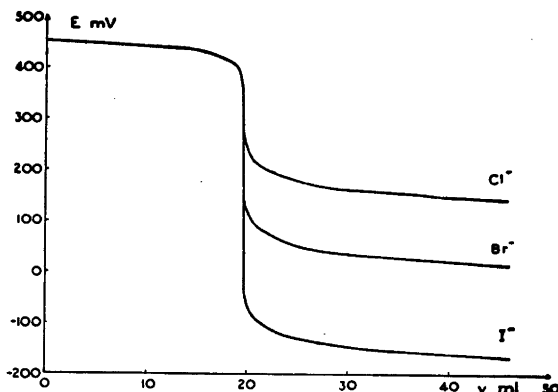


Fig. 1. Titration of 4.9 mC  $Hg_2^{2+}$  with 50 mC  $X^-$  ( $=Cl^-, Br^-,$  and  $I^-$ ).

3.2 and  $(Hg^{2+}) \approx 1.8$ ,  $E_{Hg}$  was only about 0.5 mV lower than the original value, although  $E_{Pt}$  had increased by 100 mV. Within an hour,  $E_{Hg}$  had moreover returned to a value about 0.1 mV below the original one, and afterwards remained practically constant. During the next few days, the solution was stirred continuously, and gradually approached equilibrium as is seen from  $E_{Pt}$ , which drifts slowly towards  $E_{Hg}$ .

Thus  $E_{Hg}$  kept all the time to within a few 0.1 mV of the value corresponding to the final equilibrium between the solution and Hg metal,  $(Hg_2^{2+}) = 4.94-4.95$  mC. In evaluating the potentials of Hg electrodes, we have, therefore, thought it justified to assume that, so long as there are considerable amounts of  $Hg^{2+}$  or  $Hg_2^{2+}$  ions present, the layer of solution close to the mercury is in equilibrium with the metal in accordance with (4).

#### TITRATIONS FOR DETERMINING $E_{10}$ AND $E_{1X}$

In order to obtain  $E_{10}$  and  $E_{1X}$  we made titrations with a Hg electrode and with the solutions  $S = (b - \frac{\delta}{2})$  mC  $Hg_2^{2+}$ ,  $\delta$  mC  $Hg^{2+}$  and  $T = c$  mC  $X^-$ . The general course of the  $E(v)$  curves with  $X = Cl, Br,$  and  $I$  is brought out by Fig. 1. Before the equivalence point the curves are practically identical for the three halogens; the latter part of the curve, where  $X^-$  is in excess, is highest for  $Cl^-$  and lowest for  $I^-$ , corresponding to the low solubility of  $Hg_2I_2$ .

In the first rather flat part of the curve, there is an excess of  $Hg_2^{2+}$ . In this part, the only complexes of bivalent mercury that need be considered are  $HgX^+$  and  $HgX_2$ ; the concentrations of  $HgX_3^-$  and  $HgX_4^{2-}$  can be neglected. It is, moreover, assumed that soluble complexes of mercury (I) such as  $Hg_2X^+$  can be neglected. It can be proved that the concentration of free halogen,  $X^-$ , is negligible.

If it is observed that there may be a transition  $\text{Hg}^{2+} + \text{Hg} = \text{Hg}_2^{2+}$ ; the following equations are found to be valid:

$$(\text{Hg}_2^{2+}) + (\text{Hg}_2\text{X}_2)_{\text{solid}} + (\text{Hg}^{2+}) + (\text{HgX}^+) + (\text{HgX}_2) = (\text{Hg}^{\text{I}})_{\text{total}} + (\text{Hg}^{\text{II}})_{\text{total}} = 100 \left(b + \frac{\delta}{2}\right) (100 + v)^{-1}$$

$$2(\text{Hg}_2\text{X}_2)_{\text{solid}} + (\text{HgX}^+) + 2(\text{HgX}_2) = (\text{X})_{\text{total}} = vc (100 + v)^{-1}$$

from which it follows that

$$(\text{Hg}_2^{2+}) + (\text{Hg}^{2+}) + \frac{1}{2}(\text{HgX}^+) = [100(b + \frac{\delta}{2}) - \frac{vc}{2}](100 + v)^{-1} = -\frac{1}{2}X_e \quad (9)$$

Here  $X_e$  is the concentration of halogen in excess over that needed for forming  $\text{Hg}_2\text{X}_2$  and  $\text{HgX}_2$ . In the first part of the titration curve,  $X_e$  is negative.

The results in Table 2 make it probable that close to the electrode there is equilibrium between bivalent, monovalent and metallic mercury. Under this assumption it is found from (4) and (6) and the definitions of  $\kappa_i$  in Part I that

$$(\text{Hg}^{2+}) = k_o^{-1} (\text{Hg}_2^{2+}); \quad (\text{HgX}^+) = \kappa_1 \sqrt{k_s} k_o^{-1} \sqrt{(\text{Hg}_2^{2+})} \quad (10)$$

If we insert the values of  $\kappa_1$ ,  $k_s$  and  $k_o$  that were found later on during this investigation, we find, expressing all concentrations in mC

$$\begin{aligned} (\text{Hg}^{2+}) &= 0.0077 (\text{Hg}_2^{2+}); \quad \frac{1}{2}(\text{HgCl}^+) = 0.0024 \sqrt{(\text{Hg}_2^{2+})} \\ \frac{1}{2}(\text{HgBr}^+) &= 0.0028 \sqrt{(\text{Hg}_2^{2+})}; \quad \text{and } \frac{1}{2}(\text{HgI}^+) = 0.016 \sqrt{(\text{Hg}_2^{2+})} \end{aligned} \quad (11)$$

(The values for Br and I are preliminary). The millimolar potential  $E_{10}$  can be calculated from  $E$  by means of (1) which gives

$$E_{10} = E - 29.58 \log (\text{Hg}_2^{2+}) = E - 29.58 \log (-\frac{1}{2}X_e) + \delta E \quad (12)$$

where according to (9) and (10)

$$\begin{aligned} \delta E &= 29.58 \log \left[-\frac{1}{2}X_e (\text{Hg}_2^{2+})^{-1}\right] = 29.58 \log \left[1 + (\text{Hg}^{2+}) (\text{Hg}_2^{2+})^{-1} + \frac{1}{2}(\text{HgX}^+) (\text{Hg}_2^{2+})^{-1}\right] \\ &\approx 12.85 \left[(\text{Hg}^{2+}) (\text{Hg}_2^{2+})^{-1} + \frac{1}{2}(\text{HgX}^+) (\text{Hg}_2^{2+})^{-1}\right] = \\ &= 12.85 k_o^{-1} + 6.42 \kappa_1 k_o^{-1} \sqrt{k_s} (\text{Hg}_2^{2+})^{-\frac{1}{2}} \end{aligned} \quad (13)$$

As  $(\text{Hg}_2^{2+})$  is only slightly smaller than  $(-\frac{1}{2}X_e)$ , the correction  $\delta E$  is rather small. By inserting the numerical values into (12) we find *e. g.*:

$(\text{Hg}_2^{2+}) = 4 \text{ mC}$      $\delta E = 0.115 \text{ mV}$  for Cl and Br,    0.20 mV for I  
 $(\text{Hg}_2^{2+}) = 1 \text{ mC}$                     0.13 mV for Cl and Br    0.30 mV for I  
 $(\text{Hg}_2^{2+}) = 0.25 \text{ mC}$                 0.16 mV for Cl and Br    0.50 mV for I    (14)

At  $v = 0$ , before any  $X^-$  has been added,  $\delta E$  is in all cases 0.10 mV.

Table 3 gives a few typical titrations of  $\text{Hg}_2^{2+}$  with  $\text{Cl}^-$ . The constancy of  $E_{10}$  shows that our fundamental assumptions are probably true, and especially that complexes  $\text{Hg}_2\text{Cl}^+$  are not formed in considerable amounts.

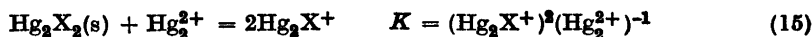
Table 3. Titrations for  $E_{10}$  and  $E_{1X}$ .  
 $S = 4.832 \text{ mC Hg}_2^{2+}$ ,  $0.040 \text{ mC Hg}^{2+}$ .  
 $T = 50.00 \text{ mC Cl}^-$ .

v ml	$\frac{1}{2} X_e$ mC	29.58 log ( $\text{Hg}_2^{2+}$ ) mV	E mV					E average	$E_{10}$
			CE »A»		CE »G»				
0	4.872	20.24	453.85	453.9	453.7	454.8	454.9	454.8 <sub>3</sub>	434.5 <sub>9</sub>
2	4.286	18.59		452.2	452.1	453.1	453.1	453.1 <sub>3</sub>	434.5 <sub>4</sub>
4	3.723	16.78		450.4	450.4	451.4	451.3	451.3 <sub>8</sub>	434.6 <sub>0</sub>
6	3.181	14.75		448.35	448.3	449.3	449.3	449.3 <sub>1</sub>	434.5 <sub>6</sub>
8	2.659	12.44		446.0	446.0	446.9	446.9	446.9 <sub>5</sub>	434.5 <sub>1</sub>
10	2.156	9.75	443.4	443.3	443.3	444.7	444.2	444.3 <sub>8</sub>	434.6 <sub>3</sub>
12	1.671	6.50			440.2	441.1	440.9	441.0 <sub>7</sub>	434.5 <sub>7</sub>
15	0.975 <sub>7</sub>	-0.45	433.3					(434.3)	(434.7 <sub>5</sub> )
17	0.531 <sub>6</sub>	-8.26	425.5					(426.5)	(434.7 <sub>6</sub> )
19	0.102 <sub>5</sub>	-29.45	403.9					(404.9)	(434.3 <sub>5</sub> )
		59.16 log $X_e$ $X_e$ mV							$E_{1X}$
20	0.213	-39.70	239.9					(240.9)	(201.2 <sub>0</sub> )
21	0.625	-12.08	212.85					(213.8 <sub>5</sub> )	(201.7 <sub>7</sub> )
30	4.043	35.89	164.7					(165.7)	(201.5 <sub>9</sub> )
35	5.745	44.92	155.9	155.7				156.8 <sub>0</sub>	201.7 <sub>2</sub>
40	7.326	51.16	149.1	149.2	150.0	150.8	150.8	150.5 <sub>8</sub>	201.7 <sub>4</sub>
45	8.797	55.87		144.3	144.3	145.3		145.3 <sub>0</sub>	201.1 <sub>7</sub>
50	10.171	59.59		140.5	140.9	141.9	141.9	141.8 <sub>0</sub>	201.3 <sub>9</sub>

For each value of  $v$  (the volume added),  $X_e$  and  $29.58 \log (\text{Hg}_2^{2+})$  have been calculated with the aid of (9), (12) and (14). The emf's were measured with two different CE's, »A» and »G»; Before the average was taken, 1.0 mV was added to the emf's with »A». Average of the values for 0—12 ml and 30—50 ml:

$$E_{10} = 434.5_7, E_{1X} = 201.5_2$$

The equilibrium conditions for  $\text{Hg}_2\text{X}^+$  would be



The  $\text{Hg}_2\text{X}^+$  present would cause an additional term  $\frac{1}{2}(\text{Hg}_2\text{X}^+)$  to the left in (9) and thus an addition to  $\delta E$

$$\begin{aligned} \delta' E &= 29.58 \log [1 + \frac{1}{2}(\text{Hg}_2\text{X}^+)(\text{Hg}_2^{2+})^{-1}] \approx 6.42 (\text{Hg}_2\text{X}^+)(\text{Hg}_2^{2+})^{-1} = \\ &= 6.42 \sqrt{K} (\text{Hg}_2^{2+})^{-\frac{1}{2}} \end{aligned} \quad (16)$$

If the amount of  $\text{Hg}_2\text{X}^+$  were considerable, there would be a decrease in the calculated  $E_{10}$  between  $v = 0$  (where no X has been added) and, for example,  $v = 2$  ml. Actually no such decrease could be proved to exist for Cl, Br or I. In any case it never seemed to amount to as much as 0.2 mV, which according to (16) means that  $K$  is less than  $5 \cdot 10^{-6}$ . Even if this value were attained, the  $k_{12}$  calculated in Part II<sup>2</sup> for  $\text{Hg}_2^{2+} - \text{Cl}^-$  and  $\text{Br}^-$  would not be significantly changed. (The value of  $k_{12}$  for  $\text{I}^-$  is in any case rather uncertain). In the  $\text{E}_{\text{max}}$  titration to be described in Parts IV and V, no error at all would be caused by disregarding  $\text{Hg}_2\text{X}^+$ .

During our investigations the difference  $E_{20} - E_{10}$  was determined on several occasions, using different stock solutions and different CE:s. The results are summarized in Table 4; each pair of values given was measured with the same CE and within a short time interval.

Table 4. Measurements of  $E_{20}$  and  $E_{10}$ .

Month	CE	$E_{20}$	$E_{10}$	$E_{20} - E_{10}$
7. 1945	»G»	559.7	434.7	125.0
»	»A»	559.6	434.8	124.8
5. 1946	»G»	559.1	434.0	125.1
»	»G»	559.2	434.5	124.7
7. 1946	»A»	559.1	433.6	(125.5)*
»	»G»	559.3	434.6	124.7
8. 1946	»A»	558.3	433.6	124.7
»	»A»	558.6	433.6	125.0
»	»G»	559.5	434.6	124.9
9. 1946	»A»	559.2	433.9	(125.3)*
10. 1946	»A»	558.9	433.9	125.0

Average  $124.9 \pm 0.2$

We have excluded the measurements of  $E_{20}$  made with one particular stock solution of  $\text{Hg}_2^{2+}$  which was prepared in November, 1945, and proved later on to have been contaminated.



With two exceptions, marked with an asterisk, the difference  $E_{20} - E_{10} = 59.16 \log k_0$  is seen to lie within the limits

$$59.16 \log k_0 = 124.9 \pm 0.2 \text{ mV} \quad (17)$$

With the first less accurate apparatus (see Part I), Inger Brattsten, *legitimerad apotekare*, found  $E_{20} - E_{10} = 558.0 - 432.7 = 125.3 \text{ mV}$ , whereas Mrs Inga Westöb found  $558.0 - 433.4 = 124.6 \text{ mV}$ . These values are seen not to be very far from our final average.

From (17) follows

$$\log k_0 = 2.111_2 \pm 0.003_4 \quad ; \quad k_0 = 129.2 \pm 1.0 \quad (18)$$

This constant has previously been determined analytically by Ogg (1898)<sup>3</sup> who found 100—120 (the temperature was not mentioned) and by Abel (1901)<sup>4</sup> who found 120 at 25° C. Latimer<sup>5</sup> calculated  $k_0$  for infinite dilution from the standard potentials of mercury; he found 81, but as the extrapolation of the redox potential to infinite dilution is uncertain to within about 5 mV, this  $k_0$  is not very accurate. As the activity factors of the two bivalent ions can be expected approximately to cancel out one another,  $k_0$  should not vary very much with the ionic strength. However, the effect of varying acidity may be considerable and this is probably the chief reason for the uncertainty of an extrapolation to infinite dilution.

From (17) we find, standardizing  $E_{10}$  to 434.5 mV

$$E_{10}^{st} = 434.5 \text{ mV} \quad E_{20}^{st} = 559.4 \pm 0.2 \text{ mV} \quad (19)$$

From (8) and (19) we find for any Hg electrode

$$E^{st} = 496.95 (\pm 0.10) + 29.58 \log (\text{Hg}^{2+}) \quad (20)$$

This expression will prove useful in subsequent work.

#### $E_{1X}$ AND $k_s$ FOR $\text{Hg}_2\text{Cl}_2$

After the equivalence point, there is a new flat part of the titration curve  $E(v)$  in Fig. 1. From this part of the titration it is possible to calculate  $E_{1X}$  and thus  $k_s$  for  $\text{Hg}_2\text{X}_2$  by means of (2) and (6). The excess of halogen

$$X_s = [vc - 200(b + \frac{\delta}{2})] (100 + v)^{-1} \quad (9a)$$

is positive and one might ask if it is permissible to assume  $X_s = X$ , (or  $(X^-)$ , the concentration of free  $X^-$  ions). Certainly all previous experimental evidence speaks against the existence of considerable amounts of soluble complexes  $Hg_2X_3^-$  and the like at moderate  $X^-$  concentrations. However, in equilibrium with Hg metal, solid  $Hg_2X_2$ , and  $X^-$  there is always a certain amount of  $HgX_2$ ,  $HgX_3^-$ , and  $HgX_4^{2-}$ , and it can be shown that

$$X_s = (X^-) + (HgX_3^-) + 2(HgX_4^{2-}) = X(1 + \kappa_3 k_s k_o^{-1} + 2 \kappa_4 k_s k_o^{-1} X) \quad (21)$$

If the numerical values of the equilibrium constants for Cl are inserted, it is found that the two constant factors to the right in (21) are about  $10^{-5}$  and  $2 \cdot 10^{-7} \text{ mC}^{-1}$ , and can thus be neglected. Consequently it seems permissible to use  $X_s$  instead of  $(X^-)$  in (2).

In the latter part of Table 3 are given particulars of a few titrations, whereas Table 5 gives average values of  $E_{10}$  and  $E_{1X}$  for a number of titrations. As in

Table 5. Measurements of  $E_{10}$  and  $E_{1X}$ .

Month	$E_{10}$	$E_{1X}$	$E_{10} - E_{1X}$
7. 1945	434.7	201.9	232.8
12. 1945	434.3	201.1	233.2
"	434.2	200.9	233.3
6. 1946	435.5	202.2	233.3
7. 1946	433.6	200.5	233.1
"	434.6	201.5	233.3
Average			$233.1 \pm 0.3$

each titration the  $E_{1X}$  values for different  $v$  often differ by 0.2—0.3 mV, whereas the difference in  $E_{10}$  or  $E_{20}$  in the same titration are usually only 0.1 mV, it seems safe to give here broader limits of error,

$$E_{10} - E_{1X} = -29.58 \log k_s = 233.1 \pm 0.3 \text{ mV} \quad (22)$$

from which follows

$$\log k_s = 0.120 \pm_{\frac{1}{3}} 0.010 - 8;$$

$$k_s = (1.32 \pm 0.03) \cdot 10^{-8} \text{ mC}^3 = (1.32 \pm 0.03) \cdot 10^{-17} \text{ C}^3 = (Hg_2^{2+}) (Cl^-)^2 \quad (23)$$

$$E_{1X}^{st} = 201.4 \pm 0.3 \text{ mV} \quad (24)$$

According to Brodsky and Scherschewer (1926) the activity product of  $\text{Hg}_2\text{Cl}_2$  at  $25^\circ\text{C}$  is  $K_s = 1.15 \cdot 10^{-18}$ . If this value is assumed to be correct, the product of the activity factors in our solutions should be about 0.1, which seems reasonable.

*Experimental note:* After the equivalence point, the emf was at first higher than the final value, which was not attained until after several hours. Our observations could be explained by the assumption that the precipitate is at first very fine-grained and therefore more soluble than are larger grains. Thus when the solution was stirred before equilibrium had been reached, the potential was too high (both small and large grains smashed against the mercury surface). If the stirrer was stopped, the emf sank to a value close to the final equilibrium emf, as the larger grains are the first to sink down to the mercury surface.

In one instance the titration of  $\text{Hg}_2^{2+}$  was started in the evening. When a certain excess of  $\text{Cl}^-$  had been added, after about an hour the emf was 181.0 mV with vigorous stirring, 180.8 mV with moderate stirring, and 180.6 mV if the stirring was stopped for a while; these emf:s could be reproduced at will. Next morning, the emf was still 180.6 mV without stirring but increased to 180.7 mV if a vigorous stirring was applied.

#### SUMMARY

Under the experimental conditions chosen:  $25^\circ\text{C}$ ,  $(\text{H}^+) = 10\text{ mC}$ ,  $(\text{X}^-) + (\text{ClO}_4^-) = 500\text{ mC}$ , the following »millimolar potentials» (see 1—3) were found:

$$E_{10}^{\text{st}} = 434.5 \text{ (standard value)}, E_{20}^{\text{st}} = 559.4 \pm 0.2, E_{\text{IX}}^{\text{st}} = 201.4 \pm 0.3 \text{ (for Cl)}$$

The following equilibrium constants were calculated:



It was shown that a mercury electrode in a solution containing  $\text{Hg}^{2+}$  and  $\text{Hg}_2^{2+}$  quickly acquired the potential corresponding to the final equilibrium between the solution and Hg metal. During a titration of  $\text{Hg}_2^{2+}$  with halogen  $\text{X}^-$ , corrections should be made for the presence of  $\text{Hg}^{2+}$  and its complexes with  $\text{X}^-$ . Expressions are given for these corrections. No appreciable amounts of soluble complexes  $\text{Hg}_2\text{X}^+$  could be detected.

The effect of stirring on the electrode potential of Hg in a newly precipitated suspension of  $\text{Hg}_2\text{X}_2$  in an  $\text{X}^-$  solution is discussed.

## REFERENCES

1. Sillén, L. G. *Svensk Kem. Tid.* **58** (1946) 52 (Part I).
2. Sillén, L. G., and Infeldt, G. *Svensk Kem. Tid.* **58** (1946) 61 (Part II).
3. Ogg, A. *Z. physik. Chem.* **41** (1898) 709.
4. Abel, E. *Z. anorg. Chem.* **26** (1901) 373.
5. Latimer, W. M. *Oxidation Potentials*. New York (1938) 164.
6. Brodsky, A. E., and Scherschewer, J. M. *Z. Elektrochem.* **32** (1926) 1.

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